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Verification of the whitetopping thickness design procedure for asphalt concrete overlaid Portland cement concrete pavements

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Verification of the whitetopping thickness design procedure for asphalt concrete overlaid
Portland cement concrete pavements

by

Toni Raenette Tabbert

A thesis submitted to the graduate faculty
in partial fulfillment of the requirements for the degree of
MASTER OF SCIENCE

Major: Civil Engineering (Geotechnical and Structural Engineering)

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2006

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1.0 INTRODUCTION

Iowa is one of few states with a large number of Portland Cement Concrete (PCC) pavements. Many of these pavements were designed with an initial design life of 20 years. By the 1970's these pavement systems had either reached or exceeded their design life. In order to rehabilitate these old pavements multiple layers of Asphalt Concrete (AC) were placed over the existing PCC slabs which increased the life of the roadway for about 10 to 15 years [1]. However, there was a need for an alternative with a longer life and lower life-cycle cost. With improvements in paving technology such as the slipform paver and the ability to obtain high early age strength, PCC overlays soon became that alternative.

Since PCC overlays are a fairly new concept to the paving industry, their design and construction has been based on empirical methods. Recent research has provided engineers with more mechanistic design possibilities. Before these mechanistic design procedures can be applied to existing AC overlaid PCC (AC/PCC) pavements, engineers need a practical means to determine the properties of the composite pavement. Also, many of the current overlay design procedures were developed for an existing single placed layer of pavement and are not applicable to the two layered AC/PCC pavements. In the *TR 511* [2] report, a method was developed so that the single placed layer concept could be applied to the analysis and design of overlays for AC/PCC pavements.

1.1 Project Background

In 1994, an Ultra Thin Whitetopping (UTW) was placed on a 7.2 mile segment of Iowa Highway 21, near Belle Plain, Iowa. When the highway was constructed, it was the largest UTW in the United States. This research focused on the condition of the bond at the interface between the PCC overlay and the existing AC pavement overtime, with consideration given to a combination of various factors. These factors include varying the depth of the overlay, joint spacing, surface preparation, incorporation of various types of fiber reinforcement, and joint preparation/sealing [3].

In 2002, the Iowa Department of Transportation (IDOT) initiated a second project to examine and verify the findings of the Iowa Highway 21 research. The project is a 9.6 mile long segment located north of Manchester, Iowa along Iowa Highway 13. This highway was originally built in 1931 and constructed as an 18 ft wide, thickened edge PCC pavement with a 7" depth at the center line and a 10" depth along the outer edge. In 1964, the PCC driving surface was rehabilitated with a 2" AC overlay. In 1984, it was overlaid again with an additional 3" of AC and widened from 18 ft to 24 ft. In 2002, Iowa Highway 13 was rehabilitated with either a 3.5" or a 4.5" PCC overlay. When the highway was overlaid in 2002 it was still in good structural condition, but cracking and deterioration of the AC overlay was extensive. In addition to the overlay, a 5 ft widening unit was placed on each side of the roadway extending the driving surface to 28 ft wide [1]. The proposed cross section of the road way is shown in Figure 1-1.

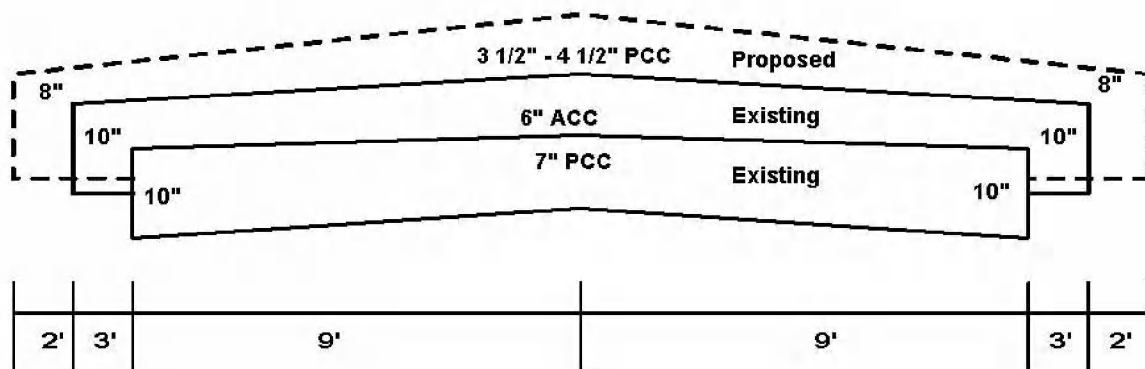


Figure 1-1 Cross-Section of Iowa Highway 13

The Iowa Highway 21 project identified outer boundaries for each of the variables (panel size of 2', 4', 6', and 12' squares, depth of overlay 2", 4", 6", and 8") in terms of performance. Panel sizes of 4.5', 6', and 9' squares and overlay depths of 3.5" and 4.5" were used to further delineate the relationships in the Iowa Highway 13 project. Data collected on deflections and performance (visual distress) from the Iowa Highway 13 project is utilized for the analysis and verification of design concepts discussed in this research.

The study presented here is an extension of previous research. Its purpose was to investigate and verify existing methodologies related to analysis and design of PCC overlays. It also presents modifications that may be used in future research.

1.2 Objectives

The primary objective of this research was to review a previously developed PCC overlay design procedure and apply plate theory to analyze displacements and overlay material stresses. In order to achieve this objective, the following sub-objectives were also considered:

- Apply the backcalculation procedure developed by Hall and Darter [4] to determine the pavement properties of an existing AC/PCC pavement and the modulus of subgrade reaction of its foundation
- Develop multiple finite element models to verify the procedure for an “equivalent” plate based on two layered AC/PCC pavements outlined in *Structural Evaluation of Base Layers in Concrete Pavement Systems* [5]
- Develop an analytical model to verify deflection and stress calculations for a two layered AC/PCC pavement based on Ioannides [5] “equivalent” plate method
- Modify/revise the previously developed methodology for application to an existing PCC overlaid AC/PCC pavement system
- Develop an analytical finite element model to investigate the application of modified calculations to three layered pavement systems

1.3 Research Approach

To obtain the objectives mentioned above, the following tasks were performed:

- Study field performance of Iowa Highway 13 considering on the following conditions:
 - Distress of the roadway

- Structural condition of the roadway
- Evaluation of the soil and drainage conditions
- Collection of data regarding the structural condition of the pavement using a Falling Weight Deflectometer (FWD) prior to overlay
- Collection of field data for the determination of soil properties
- Determination of information regarding properties of the roadway and its consecutive layers.
- Calculation of an “equivalent” thickness for the composite pavement before and after overlay placement
- Determination of deflections and stresses in single layer and multi-layered pavement systems using Ioannides “equivalent” plate method [5]
- Comparison of the calculated results with values obtained from Finite element models

2.0 LITERATURE REVIEW

2.1 Fundamental Behavior of Whitetopping Pavements

The behavior of Thin Whitetopping (TWT) and UTW pavements is uniquely different from those of conventional PCC and HMA pavements. TWT and UTW are designed and constructed with the assumption that the whitetopping is fully bonded to the existing pavement, resulting in a composite structure [7]. The condition of the bond at the interface significantly affects how traffic and environmental loads are carried.

How stresses are distributed in a bonded system versus an unbonded system is illustrated in Figure 2-1. The composite action of the bonded system causes stresses in the top PCC layer to be considerably lower when compared to the unbonded case. Therefore, thinner whitetoppings can be designed for fully bonded pavement systems [8].

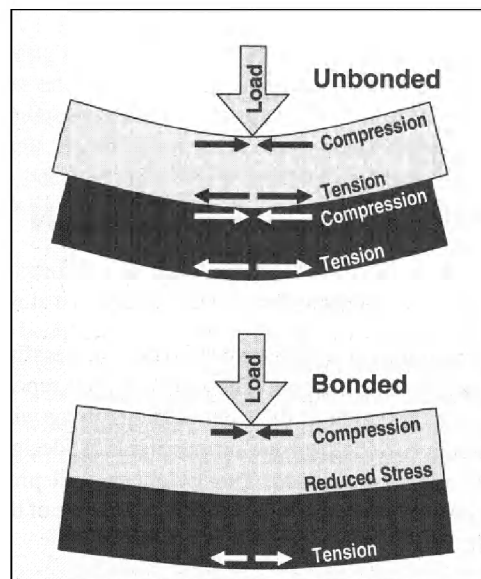


Figure 2-1 TWT and UTW Behavior under Flexural Loading [6]

This type of stress distribution is also applicable to AC/PCC and PCC overlaid on to AC/PCC (PCC/AC/PCC) pavements. However, during construction only a partial bond is

normally achieved. As a result the actual stresses occurring in a composite pavement will lie somewhere between the bonded and unbonded cases.

2.2 Pavement Whitetopping Studies

In the 1900's, the Portland Cement Association (PCA) began a study to develop mechanistic UTW pavement design guidelines. As part of this experiment, researchers studied the theoretical behavior of UTW pavements, performed field load testing, and developed a 3-dimensional (3-D) model of the PCC overlaid AC roadway. The parametric study using the 3-D model considered pavement characteristics such as load position, alignment of cracks in the existing AC with the edges of the new PCC slab, load transfer, and bond condition between the PCC slab and AC pavement. Stresses were evaluated within three locations of the pavement system; at the surface of the PCC slab, at the bottom of the PCC slab (i.e. at the interface), and at the bottom of the AC layer. The PCA study showed the bond condition significantly affected the degree of stress experienced by the pavement when subjected to load. It was also shown that stresses were affected by the condition of the existing AC. Results from the analytical study were confirmed with field instrumentation and load testing which lead to a reasonable design procedure for UTW's [9].

As part of the PCA study, the Colorado DOT (CDOT) constructed two whitetopping projects. Using the findings from these pavements the CDOT implemented a second project in 2001. Similar to the PCA study the CDOT experimental pavements were instrumented and load tested. However, these pavements were located in areas with a higher traffic volume. As a result a thicker whitetopping was constructed. Unlike the design guidelines that resulted from the 1998 project, the revised design procedure took into consideration the effects of slab thickness and joint spacing [10].

2.2.1 Other Pavement Design Methodologies

The following methodologies were described in report *TR-511* [2].

- Transtec Overlay Design [11]
- Illinois (Riley et al. 2005) [12]

The details of these methodologies are not described here due to the nature of the objectives for this thesis, shown above.

2.3 Evaluation of an Existing AC/PCC Pavement

AC overlaid concrete pavements are one of the most difficult types of pavements to evaluate structurally. This is due to the complex behavior of the composite structure and the lack of knowledge of how to interpret the structural analysis results. In recent research Hall and Darter developed a structural evaluation method that could be applied to AC/PCC pavements. This procedure uses deflection data measured on an AC/PCC pavement to backcalculate the elastic moduli of the PCC slab and its foundation. Hall and Darter also state that backcalculation results can be used to identify the amount of deterioration present in the existing PCC slab [4].

2.3.1 Data Collection

Before the type of rehabilitation method is selected, evaluations considering a pavements function, structural condition, drainage, and condition of the AC material are performed. Assessment of the pavement is done in the form of distress surveys, nondestructive deflection testing (NDT), and materials sampling and testing. Of the three methods, distress surveys are the most useful to engineers [4].

Nondestructive deflection testing is done with the use of a Falling Weight Deflectometer (FWD). For the backcalculation method described in this paper, a target load of 9000 pounds is used and deflection measurements are taken from sensors located at the center of the load plate (d_0) and at 12 (d_{12}), 24 (d_{24}), and 36 (d_{36}), inches from the center of the load plate [4]. Deflections taken from these locations are then used to calculate the area of the deflection basin. A representation of the deflection basin and how it relates to FWD loading can be seen in Figure 2-2.

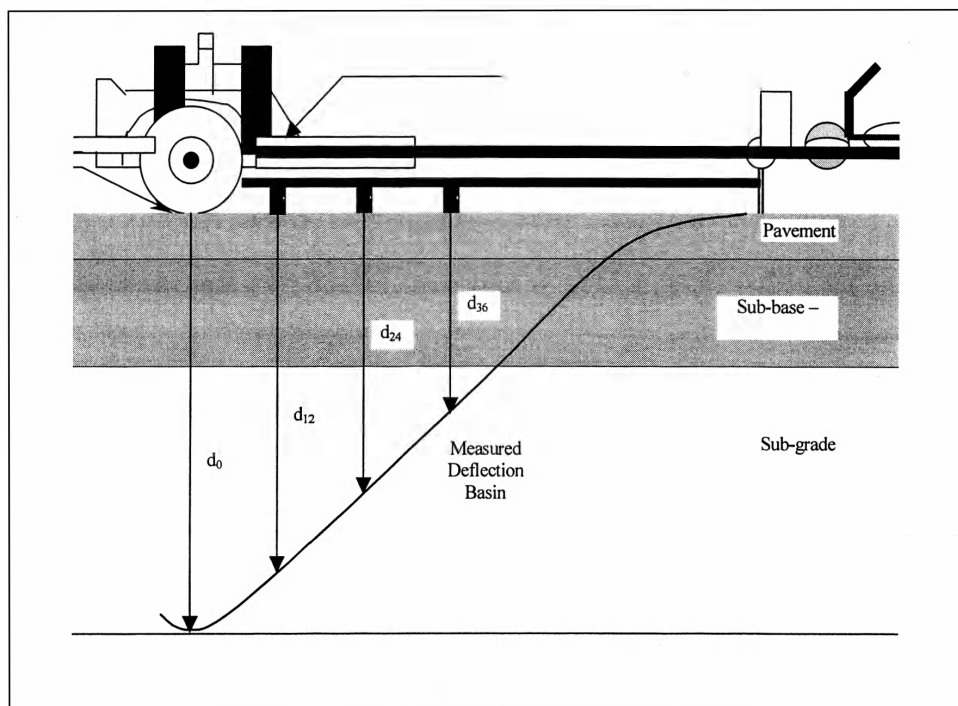


Figure 2-2 Typical Deflection Basin [13]

2.4 Development of Ioannides “Equivalent” Plate Method

Closed form analytical solutions have been used for PCC pavement design and analysis for the past 75 years. The same restrictive assumptions that led to Westergaard’s equations also govern the development of mechanistic-based design procedures in use today. These assumptions are listed below;

- Slab size has no effect on the pavement system
- The pavement system is only a single slab panel, therefore it experiences no load transfer
- The pavement system is constructed as a single-placed layer (SPL) with no base or subbase
- The pavement system rests on a foundation with no rigid bottom (semi-infinite foundation)
- The pavement system experiences a single tire print and multiple wheel loads are not considered
- The pavement system experiences no temperature or moisture effect (no curling and warping)

In concrete pavement construction, the actual behavior of the pavement system disobeys all of these assumptions. Therefore many analytical solutions must be adjusted before a reasonable design can be developed. In PCC pavement design it is common to consider feasible alternatives such as the use of AC. The single placed layer assumption does not allow for this alternative because AC pavement construction utilizes either a base or subbase, creating a multi-layered pavement system [5].

In an effort to accommodate multi-layered pavements, an analysis and design procedure based on layered elastic theory was considered [14]. Although the layered elastic theory proved to be useful, it was unable to account for the occurrence of curling and warping experienced by a pavement slab during temperature changes. Originally, the design of single placed layer systems accommodated for this phenomenon by utilizing plate theory based designs. It was suggested by Odemark in the development of his “equivalent thicknesses method” that the layered elastic theory could be used as an extension of plate theory based designs [15].

This led to the development of an analysis procedure that incorporates the use of an “equivalent” plate to determine maximum responses experienced by multi-layered pavements. The proposed procedure starts by considering two placed layers and their

foundation, as a composite plate resting on an elastic foundation (liquid or solid). It then proposes that there exists an imaginary SPL or plate of homogeneous material resting on the same elastic foundation. This SPL is also known as the “equivalent” plate. It is assumed that the “equivalent” plate is a representation of the composite plate. Therefore, material properties, deformation, and moment carried by both systems are assumed to be equal [5].

In order to develop an analytical process that uses the “equivalent” plate to determine maximum responses in a composite pavement system the following assumptions must be made:

- The development of the “equivalent” plate is based on medium thick plate theory [16]
- The “equivalent” plate is of uniform cross section and experiences elastic bending
- The layers of the composite plate do not separate in the vertical direction during bending
- Deformation of the “equivalent” plate mimics the deformation of the composite plate
- Poisson’s ratio is equal to a single value in both the composite plate and the “equivalent” plate
- The total moment acting on the composite plate is equal to the moment acting on the “equivalent” plate
- The total flexural stiffness of the composite plate is equal to that of the “equivalent” plate
- The material properties of the “equivalent” plate are represented by the material properties of the composite plate

A more detailed description of the analytical process can be found in the paper *Structural Evaluation of Base Layers in Concrete Pavement Systems* [5]

2.5 Finite Element Modeling Techniques for Composite Pavements

Finite element programs based on traditional theories of analyzing thin plates on Winkler foundations such as ISLAB2000, J-SLAB, and KenPAVE, have been used to

analyze pavements. These programs are successful in the analysis of pavements with uniform slab thicknesses, multiple layers, different slab sizes, and various other criteria. Although, the 2-D model utilized in this research was an adequate verification method for a single placed layer it was not adequate for the multilayered systems. Therefore, an alternate 3-D model was developed to supplement the analysis of the multi-layered systems. In this research, the analysis package ISLAB2000 was used for the 2-D model and ANSYS was used for the 3-D model.

2.5.1 Modeling of Concrete and Asphalt Layers

In a composite pavement the AC and PCC can be modeled by using eight node elements, also known as brick elements. Elements with a larger number of nodes, i.e. higher order elements, could also be utilized. Using a higher order element, results in an increase of computational resources. To reduce the computational need and maintain accuracy, 8-node brick elements including “extra displacement functions” can be used [17]. Since parasitic shear can result from the assumed displacement functions associated with the formulation of the 8-node solid element, extra displacement function are used to correct for this problem and enable the element to accurately represent the bending effects of the structure. 8-node solid elements with extra displacement functions were used to model the representation of Iowa Highway 13 investigated by this research.

2.5.2 Foundation Modeling Techniques

Pavement analysis and design employs three different types of foundation modeling; liquid, solid, and layered. The majority of finite element programs utilized today are based on the liquid foundation. This is because liquid foundation models require very little computer time to solve.

The force-deflection relationship of the liquid foundation is characterized by an elastic spring. The term “liquid” is used to indicate that the foundation’s deformation under a slab is similar to how water deforms under a boat [18]. The liquid foundation is also known as a Winkler foundation which is shown in Figure 2-3.

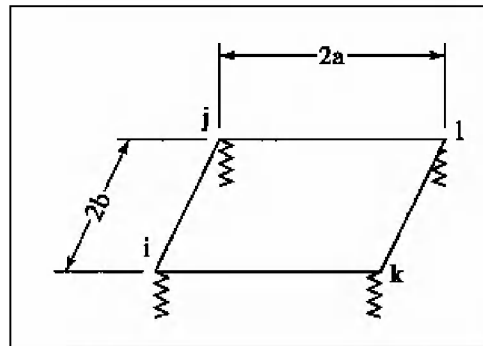


Figure 2-3 Liquid Foundation under a Plate Element

A more realistic type of foundation is the solid foundation also known as the Boussinesq foundation. The deflections of a solid foundation at any nodal point depend on the forces acting at all nodes and not just the forces acting at that point [18]. In the finite element modeling section presented later an 8-noded element was used to represent the solid foundation.

3.0 MODELING OF IOWA HIGHWAY 13

As described in previous sections the purpose of this work is to verify simplified structural analysis methods used in the analysis of multi-layered pavements such as Iowa Highway 13. Although there are several two dimensional (2-D) and three dimensional (3-D) finite element packages available, ISLAB2000 (2-D) and ANSYS (3-D) were chosen for the modeling of the composite pavement. This was due to their availability and time requires for this study.

3.1 Modeling of Composite Pavement for Finite Element Analysis

In order to verify the structural analysis method previously described in Chapter 2, three finite element models representing an “equivalent” plate, an AC/PCC pavement and a PCC/AC/PCC pavement were needed. In the work presented here, two dimensional and three dimensional modeling techniques are used. For the two dimensional modeling of the “equivalent” plate and AC/PCC pavement, the AC and concrete layers are represented by multiple layers of thin plates resting on a Winkler foundation. The foundation’s stiffness is designated by the modulus of subgrade reaction (k-value) of the soil. To account for the bond condition at the AC/PCC interface, ISLAB2000 allows for the selection of either fully bonded or completely unbonded.

For the three dimensional modeling, plate and solid elements were used to construct the “equivalent” plate, PCC overlay, AC, PCC base, and soil subgrade. When using solid elements to model the soil subgrade, the k-value is not adequate and needs to be related to the soils elastic modulus (E_s) and its poisson’s ratio (ν_s). Modeling of the bond condition is done for the fully bonded cases by using common nodes at the interface between the layers. For the unbonded cases, two sets of nodes are utilized at each nodal location. To link these nodes together in the vertical direction the ANSYS program provides the “couple” command. In order to represent an unbonded pavements behavior restraints are applied only in the vertical direction and not in the horizontal directions.

3.1.1 Types of Element Used to Model Iowa Highway 13

The following is a brief description of the type of elements used in the 3-D modeling of the AC/PCC and PCC/AC/PCC pavements.

3.1.1.1 Plate Elements

SHELL63 was chosen to model the “equivalent” plate, an unbonded AC/PCC pavement and the pavement subgrade. It is an element that has both bending and membrane capabilities. Loading can be applied normal to the plane or in-plane. There are six degrees of freedom per node allowing for translations and rotations in the x, y, and z directions. The element permits for a single thickness or is allowed to vary across the element. This element allows for the soil subgrade modulus typically associated with a Winkler foundation to be represented by defining an Elastic Foundation Stiffness (EFS) [19]. This is a more convenient method to model the Winkler foundation instead of individual nodal springs.

Since solid elements do not have the EFS capabilities, the foundation can be modeled by placing a very thin layer of plate elements under the pavement structure. This permits for the effects of a foundation without increasing the stiffness of the pavement.

3.1.1.2 Solid Elements

SOLID45 was chosen for the three dimensional modeling of the various layers in the composite pavement structure. It is an 8-node brick element with 3 degrees of freedom at each node: allowing for displacement in the nodal x-, y- and z-directions. This element has plastic, creep, swelling, stress stiffening, large deflection and large strain capabilities, along

with the capability of representing orthotropic material properties. Additionally, the element is capable of supporting pressures on any surface and concentrated forces at the nodes [19].

Since the element only has 2 nodes along each edge its interpolation functions are linear. Therefore, utilizing the basic 8-node element in analysis will result in constant strains and stresses across the element. This approach is not correct when accounting for bending stresses and the use of a higher order element would produce a more accurate result. The use of higher order elements requires increased computing time for the analysis. This time can be significantly reduced by including extra shape functions in the stiffness formulation of the element [17]. When using SOLID45, ANSYS does provide this option.

3.2 Finite Element Modeling of the “Equivalent” Plate

Modeling of the “equivalent” plate was performed using ISLAB2000 which idealizes the thickness of a slab as multiple layers of thin plates. The thickness of the slab was determined to be 9.69”. The “equivalent” plate was also modeled in ANSYS, using a plate element, a single layer of solid elements and two layers of solid elements though the thickness. The foundation for the “equivalent” plate was modeled using a very thin layer of plate elements beneath the plate structure. Results of the various modeling techniques can be seen later in the analysis section of this paper.

3.3 Finite Element Modeling of the Composite System (Iowa Highway 13)

Since the purpose of the analysis presented in this work is to investigate a simplified method for structurally evaluating pavements, it was not necessary to consider the effects of a widening unit as part of the investigation. Therefore, only representative models of Iowa Highway 13 were used for the finite element modeling. The models were constructed as a single 18 ft wide by 70 ft long slab, consisting of either two layers (AC/PCC) or three layers (PCC/AC/PCC). Each layer was constructed with a uniform thickness of 7 inches for the

original PCC, 5 inches for the AC, and 3.5 inches for the PCC Overlay. Pavement variables such as slab size and temperature effects such as curling and warping are not part of this research and will not be taken into consideration.

As previously described, the PCC overlay, AC and bottom PCC layers were meshed using plate and solid elements. Modeling of the AC/PCC pavement using plate elements was constructed using a single layer of elements for both the AC and PCC layer. This was done for the two layer unbonded case only. For all other models constructed with ANSYS the overlay and AC layers were modeled with a single layer of solid elements and the bottom PCC slab was modeled using two layers of solid element though the thickness. To model the soil underneath the pavement two methods were used. The first method was to place a very thin layer of plate elements beneath the pavement structure. The second method was to model the soil using a total depth of 40 inches and four layers of solid elements through the thickness. The modeling technique of the soil using brick elements is shown in Figure 3-1. The effects for the different modeling techniques are shown later in the analysis section of this paper.

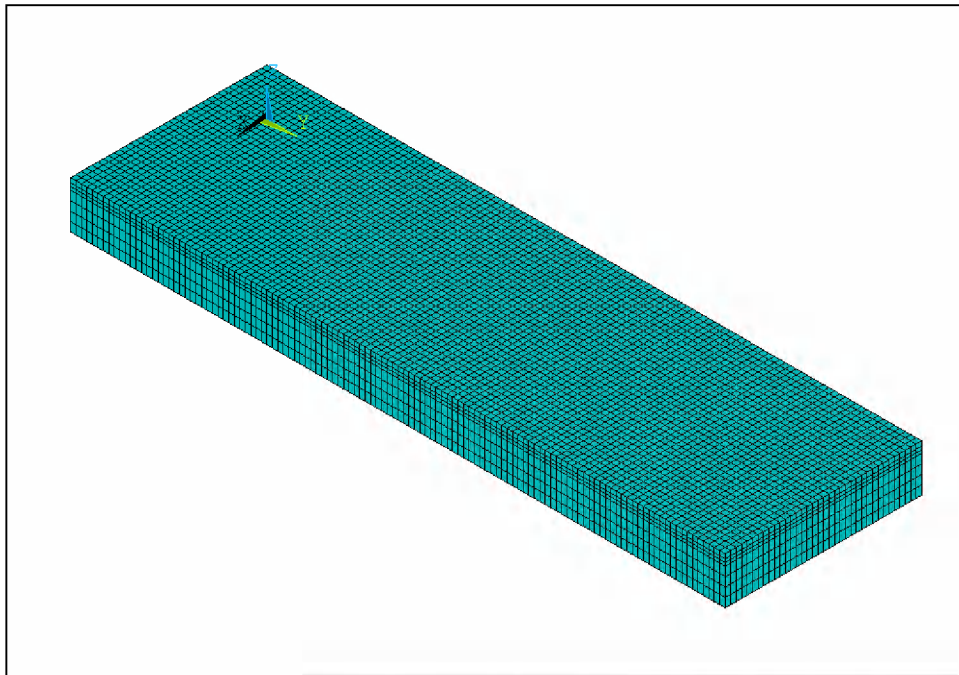


Figure 3-1 Modeling of the Pavement and Soil using Solid Elements

4.0 FIELD EVALUATION OF IOWA HIGHWAY 13

4.1 Visual Survey

Visual surveys of Iowa Highway 13 were performed before and after construction of the overlay. They were conducted prior to construction to evaluate the existing pavement and determine if an unbonded overlay was an adequate rehabilitation method. Surveys conducted after construction focused on the effects of heavy loading and freeze thaw cycles experienced by the pavement.

Results of the preconstruction survey showed that the pavement was in good structural condition with minimal cracking. There were signs of working cracks in the pavement over areas in which culverts were located. Reflective cracking was also evident throughout the roadway. Evidence of a longitudinal crack was found in the AC overlay at the location of the edge of the old PCC slab. This longitudinal crack extended the entire length of the pavement in both the northbound and southbound lanes [1].

Visual surveys performed after construction of the overlay were conducted biannually in the months of October and April. Surveys considered distresses such as longitudinal cracking, transverse cracking, diagonal cracking, fractured panels, and condition of the widening joint. Detail of the distress surveys were documented in the final report [20].

4.2 Nondestructive Deflection Testing

Deflection testing on Iowa Highway 13 was performed by the Iowa DOT with a Foundation Mechanics JLS-20-Falling Weight Deflectometer (FWD). Testing was conducted biannually, once in the fall and then again in the spring. FWD testing performed prior to the construction of the overlay was done in the outer wheel path for each lane of the roadway. A single test was done at each location and then repeated at that location for the duration of the project.

The FWD has a load plate with a radius of 6 inches. Nine deflection sensors were spaced at varying distances from the load plate with sensor one located at the center of the plate. A load magnitude of 9,000 pounds was used for the deflection testing. Figure 4-1 shows the location of the sensors in references to the load placement. [1] Air temperature was also monitored and recorded during the deflection testing. Deflection measurements and temperature results taken prior to the overlay are listed in Appendix A. These results were then used to backcalculate the pavement properties of the existing pavement.

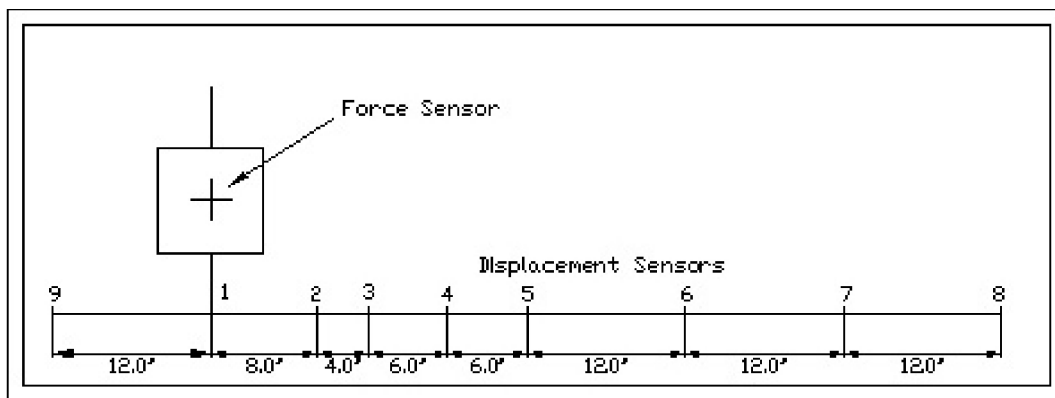


Figure 4-1 Schematic of FWD Deflection Sensors

4.3 Soil Classification

As part of this research project, soil identification was conducted along the 9.6 mile segment of Iowa Highway 13. The soil identification included consultation of the US Department of Agriculture (USDA) soil survey for Delaware County and visual soil classification was performed by the research team. Soil borings were conducted on the shoulder of the roadway approximately 1 foot from the edge of the pavement. A complete list of results from the soil classification can be seen in Appendix B. The summary of the finding from the USDA soil survey and visual classification are summarized below.

4.3.1 Soil Survey Summary

There are three different soil associations located along the 9.6 mile segment of Iowa Highway 13. These associations are the Kenyon-Clyde-Floyd association (green), the Downs-Fayette association (yellow), and the Spillville-Saude-Marshan association (blue) with the predominant association being the Kenyon-Clyde-Floyd association. This can be seen in Figure 4-2. Since the primary association is the Kenyon-Clyde-Floyd association it will be the primary focus of the research and can be described in more detail as Kenyon Loam (83B) and Clyde-Floyd Complex (391B) [21].

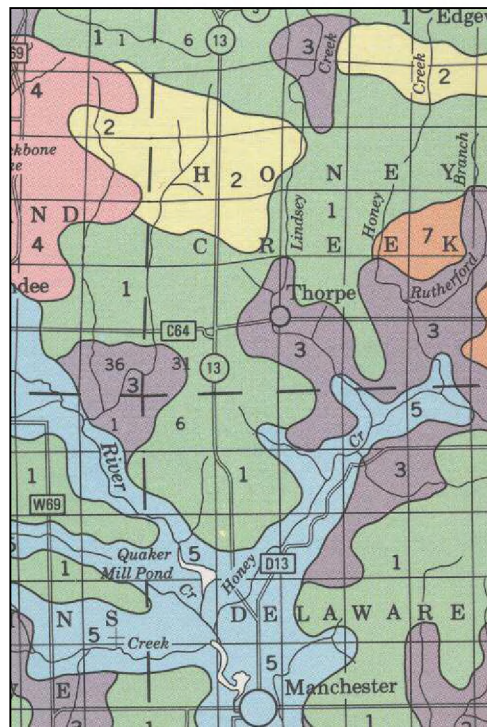


Figure 4-2 Iowa Highway 13 Soil Associations

Kenyon Loam (83B) is located on side slopes in the uplands and on long convex ridge tops. This soil is gently sloping and moderately well drained. A Kenyon Loam subsurface profile can be seen below.

- A surface layer of black loam approximately 7 inches thick and contains roughly 3 to 4 percent organic matter

- A subsurface layer of black and very dark grayish brown loam approximately 10 inches thick
- A subsoil of loam approximately 37 inches thick, with
 - An upper section of brown friable loam
 - A lower section of dark yellowish brown and yellowish brown, mottled, firm loam
- A substratum of mottled yellowish brown and grayish brown loam

Kenyon Loam is classified under American Association of State Highway Transportation Officials (AASHTO) as an A-6. Under the Unified Soil Classification System (USCS) this soil is classified as a CL.

The Clyde-Floyd Complex (391B) is located in drainage ways on glacial uplands. These soils are gently sloping and poorly drained. The Clyde soils have a slope of less than 2 percent and are located in the lowest part of the drainage way. Located in bands bordering the Clyde soils, Floyd soils have a slope of 1 to 4 percent. These two soils are not mapped separately due the complex mixing of the areas in which they occur.

A Clyde-Floyd Complex subsurface profile contains:

- Clyde soils
 - A surface layer of black loam approximately 9 inches thick
 - A subsurface layer is black clay loam approximately 14 inches thick
 - A subsoil is approximately 18 inches thick, with
 - An upper section of gray, mottled, friable loam
 - A middle section of mottled gray and yellowish brown, friable loam with a sandy stratum of approximately 1 inch thick
 - A lower section of gray, mottled, firm loam
 - A substratum of mottled gray and yellowish brown loam
- Floyd soils
 - A surface layer of black loam approximately 9 inches thick
 - A subsurface layer is black and very dark brown loam approximately 13 inches thick

- A subsoil is mottled loam approximately 18 inches thick, with
 - An upper section of dark grayish brown and friable
 - A middle section of olive brown and light olive brown loam
 - A lower section of grayish brown firm loam
- A substratum of mottled grayish brown loam

The Clyde-Floyd Complex is classified under American Association of State Highway Transportation Officials (AASHTO) as A-6 and A-7 soils. Under the Unified Soil Classification System (USCS) these soils can be classified as an OH, MH, ML, OH, CL, SM, SM-SC, and/or SC [21].

4.3.2 Visual Soil Classification Survey

At various depths, soil boring revealed yellowish brown sandy clay with gray mottling. Also, brown to very dark brown sandy clay or silt was also found. The expected soil conditions identified by the USDA soil survey correlated with the results of the visual classification.

5.0 DATA ANALYSIS

The purpose of this research is to investigate and verify existing methodologies related to the analysis and design of PCC overlays. One of those methodologies, developed by Ioannides, proposes that stresses determined from an imaginary “equivalent” plate can be used to calculate deflections and stresses within a composite pavement. Research presented here uses finite element modeling, based on an existing pavement structure, to verify these calculated results

Before deflections and stresses can be determined, material properties of the existing pavement are calculated. A Falling Weight Deflectometer was used to perform the deflection testing for this research project. Measurements taken from sensors located at 0, 12, 24, and 36 inches are used to determine the cross sectional area of the deflection basin, modulus of subgrade reaction (k_s), and the elastic modulus of the PCC slab (E_{PCC}). Corrections were made to the maximum deflection under the load to account for slab size effects and compression in the AC due to loading. These values are then used to develop the various models used in this research.

5.1 Determination of Properties for AC/PCC and PCC/AC/PCC Pavements

5.1.2 AC Elastic Modulus

A large portion of the total measured deflection of an AC/PCC pavement can be attributed to the vertical compression experienced by the AC layer under the FWD load. To determine the amount of compression in the AC layer the AC elastic modulus (E_{AC}) is calculated. The method outlined below uses the Asphalt Institute’s (AI) equation for the AC elastic modulus [22]. Shown in equation 1, this equation is a function of mix characteristics, mix temperature, loading frequency, and is considered to be very reliable for dense-graded AC mixes made up of gravel or crushed stone aggregates [23].

$$\begin{aligned}
\log E_{AC} = & 5.553833 + 0.028829 \left(\frac{P_{200}}{F^{0.17033}} \right) - 0.03476 * V_v \\
& + 0.070377 * \eta + 0.000005 * T_{AC}^{(1.3+0.49825*\log F)} * P_{AC}^{0.5} - \left(\frac{0.00189}{F^{1.1}} \right) \\
& * T_{AC}^{(1.3+0.49825*\log F)} * P_{AC}^{0.5} + 0.931757 * \left(\frac{1}{F^{0.02774}} \right)
\end{aligned} \tag{1}$$

Where,

E_{AC} = elastic modulus of AC, psi

P_{200} = percent aggregate passing the No. 200 sieve

F = 18 Hz for the FWD load duration of 25 to 30 milliseconds

V_v = percent air voids

P_{AC} = asphalt content, percent by weight of mix

T_{AC} = mean AC mix temperature at 1/3 depth, °F

η = absolute viscosity at 70°F, 10^6 poise

5.1.3 Effects of temperature on the AC elastic modulus

During FWD testing the temperature of the AC layer is measured in order to account for the variability of the AC resilient modulus during testing. Monitoring the AC temperature can be done by drilling a hole to the mid-depth of the AC layer, inserting liquid, and a temperature probe [4]. An alternate method to determine the temperature of the AC using the mean monthly air temperature was developed by Witczak and is shown below [22].

$$T_{AC} = MMAT \left(1 + \frac{1}{z+4} \right) - \frac{34}{z+4} + 6 \tag{2}$$

Where,

T_{AC} = mean temperature of the AC layer

MMAT = mean monthly air temperature

z = 1/3 depth from the surface of the AC, inches

5.1.4 Corrections for Determining the In Situ AC Elastic Modulus

The above equation for the elastic modulus of the AC is typically applied to new mixes. In situ AC mixes over time, can experience asphalt hardening causing a higher modulus value. On the other hand, if AC pavements have experienced large amounts of deterioration a lower modulus value will result [4]. The value for the AC modulus calculated using equation 1, is adjusted for aging using the following equations developed by Ullidtz. Equation 3 is used to determine an aged $Pen_{25^{\circ}C}$ in which $Pen_{25^{\circ}C}$ is the penetration of the binder at $25^{\circ}C$ ($77^{\circ}F$) [22].

$$\text{aged } Pen_{25^{\circ}C} = 0.65 * \text{original } Pen_{25^{\circ}C} \quad (3)$$

If there is not sufficient enough information to determine the absolute viscosity needed for equation 1, the following relationship shown in equation 4 [22] is used.

$$\eta = 29508.2 * \left(\text{aged } Pen_{25^{\circ}C} \right)^{-2.1939} \quad (4)$$

5.1.5 Deflection of the Existing PCC Slab

Using the elastic modulus of the AC, the amount of vertical compression in the AC layer is calculated. Measured deflections at d_0 are significantly larger when there is no bond between the AC layer and the PCC layer. However, the actual bond condition is typically unknown. As part of this research both bond conditions are considered. Therefore the following two equations are used to calculate the degree of compression experienced by the AC layer [4].

AC/PCC Bonded

$$d_{0_{\text{compress}}} = -0.0000328 + 121.5006 * \left(\frac{D_{ac}}{E_{ac}} \right)^{1.0798} \quad (5)$$

AC/PCC Unbonded

$$d_{0_{compress}} = -0.00002132 + 38.6872 * \left(\frac{D_{ac}}{E_{ac}} \right)^{0.94551} \quad (6)$$

Where,

$d_{0_{compress}}$ = AC compression at center of load, in

D_{ac} = AC thickness, in

E_{ac} = AC elastic modulus, psi

After the compression of the AC layer is determined, the calculated value is subtracted from the deflections measured at d_0 by the FWD, resulting in the actual deflection of the existing PCC layer (d_{0PCC}) [4].

$$d_{0PCC} = d_0 - d_{0_{compress}} \quad (7)$$

Where,

$d_{0_{compress}}$ = vertical compression of the AC layer, in

d_0 = maximum deflection at center of load plate, in

d_{0PCC} = deflection of the PCC layer at the center of the load plate, in

5.1.6 Deflection Basin of the PCC ($AREA_{PCC}$)

Now that the influence of the AC layer has been removed from the deflection measurements, the area of the deflection basin of the PCC slab is determined using equation 8 [4].

$$AREA_{PCC} = 6 * \left(1 + 2 * \left(\frac{d_{12}}{d_{0PCC}} \right) + 2 * \left(\frac{d_{24}}{d_{0PCC}} \right) + \left(\frac{d_{36}}{d_{0PCC}} \right) \right) \quad (8)$$

Where,

$AREA_{PCC}$ = area of the deflection basin, in

d_{0PCC} = deflection of the PCC layer at center of load plate, in

d_i = deflection at 12, 24, and 36 inches from the center of the load plate, in

Results from the AREA calculation are then used to estimate a radius of relative stiffness (l) which is defined as the ratio of the PCC slab to the stiffness of its foundation. These results are then used to calculate the modulus of subgrade reaction (k_s). The following equation was developed by Hall to calculate the radius of relative stiffness (l) as a function of the deflection basin [24].

$$l = \left[\frac{\ln\left(\frac{36 - AREA_{PCC}}{1812.279}\right)}{-2.559} \right]^{4.387} \quad (9)$$

5.1.7 Slab Size Correction

The above backcalculation procedure uses Westergaard's equation for deflection of an infinite plate on a dense liquid foundation. However, actual PCC slabs are too small to approximate infinite behavior. Therefore, adjustments to the deflection measured at d_0 and the calculated radius of relative stiffness are applied [25]. To determine if the adjustments are necessary the ratio of L/l is calculated where L is the least slab dimension. If the L/l resulting value is less than eight, the following corrections are applied to the maximum deflection in the PCC slab and calculated radius of relative stiffness [4].

$$AF_{d_0} = 1 - 1.0687 * e^{-0.66914 * \left(\frac{L}{l}\right)^{0.84408}} \quad (10)$$

$$AF_l = 1 - 5.29875 * e^{-2.17612 * \left(\frac{L}{l}\right)^{0.49895}} \quad (11)$$

$$d_{0adj.} = AF_{d_0} * \text{measured } d_0 \quad (12)$$

$$l_{adj.} = AF_l * \text{calculated } l \quad (13)$$

AF_{d_0} = adjustment factor for the measured d_0

AF_l = adjustment factor for the radius of relative stiffness

d_{0adj} = adjusted maximum deflection d_0 , in

l_{adj} = adjusted radius of relative stiffness

5.1.8 Dynamic Modulus of Subgrade Reaction

The radius of relative stiffness is then used to calculate the modulus of subgrade reaction using Westergaard's deflection equation and the adjusted values described above. The modulus value determined from the FWD deflection measurements is considered to be a dynamic modulus. The calculated dynamic modulus is about twice that of a modulus value determined from a static bearing plate test. In typical pavement design, modulus values are considered to be static. Therefore, values determined from this research should be halved if used for design purposes [4].

$$k_s = \left(\frac{P}{8 * d_{0adj} * l_{adj}^2} \right) \left\{ 1 + \left(\frac{1}{2\pi} \right) \left[\ln \left(\frac{a}{2 * l_{adj}} \right) + \gamma - 1.25 \right] \left(\frac{a}{l_{adj}} \right)^2 \right\} \quad (14)$$

where,

k_s = effective modulus of subgrade reaction, pci

d_{0adj} = adjusted maximum deflection d_0 , in

l_{adj} = adjusted radius of relative stiffness

P = FWD load, pounds

γ = Euler's constant, 0.57721566490

a = load radius, 5.9 inches for the FWD

5.1.8.1 Relationship between a liquid and solid foundation

For the finite element modeling previously described, two types of foundations were used for modeling the soil. The ISLAB models use a liquid elastic foundation and the ANSYS models use both liquid elastic and an elastic solid foundation. When modeling a liquid elastic foundation the modulus of subgrade reaction (k_S) value is directly inputted into the program. Modeling of the elastic solid foundation required values such as the elastic modulus (E_S) and poisson's ratio (ν_S) of the soil. Therefore, a relationship a relationship between the modulus of subgrade reaction and the elastic modulus was needed.

It is recommended by Vesic and Saxena (1974) that when computing stresses the following equation 15 be used to relate k_S and E_S . If the deflection is to be found it is recommended that only 42% of the solution from equation 15 be used. However, Huang and Sharpe (1989) determined that equation 15 is only applicable when the load is located on the interior of the slab and recommend equation 16 for loads located on the edge [18].

$$k_S = \left(\frac{E_S}{E_{PCC}} \right)^{1/3} \frac{E_S}{(1 - \nu_S^2) h_{PCC}} \quad (15)$$

$$k_S = 1.75 \left(\frac{E_S}{E_{PCC}} \right)^{1/3} \frac{E_S}{(1 - \nu_S^2) h_{PCC}} \quad (16)$$

k_S = effective modulus of subgrade reaction, pci

E_S = elastic modulus of the soil, psi

ν_S = poisson's ratio of the soil, psi

E_{PCC} = elastic modulus of the PCC slab, psi

h_{PCC} = thickness of the PCC slab, inches

An alternative equation known as the reduced Vesic equation may also be used when relating the modulus of subgrade reaction to the elastic modulus of the soil. This equation is shown in equation 17 in which B is the diameter of the bearing plate, typically taken as 30 inches. The reduced Vesic equation is impartial to the placement of a load on a pavement surface and produces comparable results to the above mentioned equations [26].

$$k_s = \frac{E_s}{B(1 - \nu_s^2)} \quad (17)$$

k_s = effective modulus of subgrade reaction, pci

E_s = elastic modulus of the soil, psi

ν_s = poisson's ratio of the soil, psi

B = diameter of the bearing plate or 30 inches

In the Field Evaluation section of this report it was shown that a significant portion of the soils located along Iowa Highway 13 were classified as CL type soils. The subgrade modulus of reaction for these types of soils can range from 125 pci to 225 pci. Therefore, the calculated k_s value of 150 pci is acceptable. The poisson's ratio for these types of soils can range from 0.3 to 0.5 [18]. In this research the averaged value of 0.4 is used for the Poisson's ratio. A table of the calculated soil elastic moduli can be seen in Table 5-1.

Table 5-1 Elastic Modulus of the Soil Summary

| | Unbonded | Bonded |
|----------------------|----------|--------|
| <u>Center Load</u> | | |
| E_s , psi | 6790 | 7100 |
| $E_{s\ 42\%}$, psi | 2850 | 2980 |
| <u>Edge Load</u> | | |
| E_s , psi | 4460 | 4670 |
| <u>Reduced Vesic</u> | | |
| E_s , psi | 3970 | 3970 |

5.1.9 Existing PCC Elastic Modulus

With the modulus of subgrade reaction determined the elastic modulus of the PCC slab may be calculated [27].

$$E_{PCC} = \frac{12 * (1 - \nu_{PCC}^2) * k * l^4}{D_{PCC}^3} \quad (18)$$

where,

E_{PCC} = estimated elastic modulus of the existing PCC, psi

ν_{PCC} = Poisson's ratio of the PCC

k = effective modulus of subgrade reaction, pci

l = adjusted radius of relative stiffness

D_{PCC} = thickness of the existing PCC slab, in

This backcalculation procedure is completed at each station where the FWD load is dropped over the length of the project. Since the PCC moduli vary considerably over the length of the project. Deflection values that produce AREA values larger than 36 are not used in calculations of the PCC moduli. In order to add a factor of safety to the design and to address the spread that can be seen in the calculated PCC modulus, a cumulative percentage plot is used [4]. Once the PCC moduli are backcalculated from the above procedure, a histogram is created using a reasonable grouping interval. The cumulative percentage is then calculated from the histogram data using the following equation:

$$\frac{\#of\ modulli \leq\ current\ interval}{total\ \#of\ moduli\ values} = \text{Cumulative Percentage} \quad (20)$$

The results are then plotted with the moduli values on the x-axis and the percentage on the y-axis. Depending on how conservative the engineer wants to make the design, a percentage is selected. Three percentages should be used depending on the level of design sought: 60% should be used for a lean design, 75% should be used for a middle of the road design, and 85% should be used for a conservative design [2].

Information provided by the IDOT estimated the compressive strength of the whitetopping layer to be 4500 psi. A complete table of results from the above described

procedure is located in Appendix C. A summary of the existing AC and PCC properties are shown in Table 5-2.

Table 5-2 Summary of Material Properties

| | Unbonded E_{PCC} , psi | Bonded E_{PCC} , psi |
|---|-----------------------------|---------------------------|
| 65% | 2600000 | 2300000 |
| 75% | 3700000 | 3100000 |
| 85% | 4500000 | 3750000 |
| Elastic Modulus of the AC, psi | 1354680 | |
| Elastic Modulus of the PCC Overlay, psi | 3823680 | |

5.2 Determination of Stresses using Ioannides “Equivalent” Plate Method

The “equivalent” plate theory was developed by Ioannides et al. as a way to evaluate the contribution of the modulus when a PCC slab is placed on top of a stabilized base [5]. In this work, this theory is applied to an AC/PCC pavement. It is proposed that stresses determined from an imaginary “equivalent” plate can be used to determine the stresses within the composite plate that it represents. First an equivalent thickness (h_e) must be determined using properties from the actual composite structure. In order to determine the thickness the assumptions outlined in section 2.5.1 must be maintained and a decision on whether the AC is fully bonded or completely unbonded from the PCC layer. Stresses within the “equivalent” plate along with its deflection are determined using either Westergaard’s equations or finite element analysis. This “equivalent” stress is then used to calculate stresses at the various interfaces of the composite pavement.

5.2.1 Evaluation of the “Equivalent” Plate for an Unbonded AC/PCC Pavement

If the AC and PCC layers are not bonded, the equation to calculate thickness of the equivalent “plate” is rather simple. For equation 20 it was assumed that the properties in the equivalent plate were equal to the properties of the AC layer.

$$h_e = \left[D_{AC}^3 + \frac{E_{PCC}}{E_{AC}} * D_{PCC}^3 \right]^{(1/3)} \quad (20)$$

where,

h_e = equivalent thickness of the existing pavement, in

D_{AC} = thickness of the AC layer, in

D_{PCC} = thickness of the PCC layer, in

E_{AC} = elastic modulus of the AC, psi

E_{PCC} = elastic modulus of the PCC, psi

The thickness and stresses determined for the “equivalent” plate (σ_e) are then used to calculate the maximum bending stress in the bottom of AC layer (σ_{AC}) using equation 21. The stresses in the bottom of the PCC layer (σ_{PCC}) are then determined using equation 22 [5].

$$\sigma_{AC} = \frac{D_{AC}}{h_e} * \sigma_e \quad (21)$$

$$\sigma_{PCC} = \frac{D_{PCC}}{E_{AC}} * \frac{E_{PCC}}{E_{AC}} * \sigma_{AC} \quad (22)$$

5.2.2 Evaluation of the “Equivalent” Plate for a Bonded AC/PCC Pavement

If the AC and PCC layers are bonded, the neutral axis of the composite plate is calculated before the equivalent thickness is determined. For equation 23 it was assumed that the properties in the equivalent plate are equal to the properties of the PCC layer [5].

$$x = \frac{E_{PCC}D_{PCC} \frac{D_{PCC}}{2} + E_{AC}D_{AC} \left(D_{PCC} + \frac{D_{AC}}{2} \right)}{E_{PCC}D_{PCC} + E_{AC}D_{AC}} \quad (23)$$

where,

- x = distance to the neutral axis, in
- D_{AC} = thickness of the AC layer, in
- D_{PCC} = thickness of the PCC layer, in
- E_{AC} = elastic modulus of the AC, psi
- E_{PCC} = elastic modulus of the PCC, psi

After the location of the neutral axis is determined the “equivalent” thickness of the plate is calculated.

$$h_e = \left\{ \begin{aligned} & D_{PCC}^3 + \frac{E_{AC}}{E_{PCC}} D_{AC}^3 \\ & + 12 \left[\left(x - \frac{D_{PCC}}{2} \right)^2 D_{PCC} + \frac{E_{AC}}{E_{PCC}} \left(D_{PCC} - x + \frac{D_{AC}}{2} \right)^2 D_{AC} \right] \end{aligned} \right\}^{(1/3)} \quad (24)$$

where,

- D_{AC} = thickness of the AC layer, in
- D_{PCC} = thickness of the PCC layer, in
- E_{AC} = elastic modulus of the AC, psi
- E_{PCC} = elastic modulus of the PCC, psi

The thickness and stresses determined for the “equivalent plate (σ_e) are then used to calculate the maximum bending stress in the top of the PCC layer (σ_{PCC}) using equation 25. Stresses in the top of the AC layer (σ_{AC}) are then determined using equation 26 [5].

$$\sigma_{PCC} = \frac{2(D_{PCC} - x)}{h_e} * \sigma_e \quad (25)$$

$$\sigma_{AC} = \sigma_{PCC} \left(\frac{E_{AC}}{E_{PCC}} \right) \left(\frac{D_{AC} + D_{PCC} + x}{x} \right) \quad (26)$$

5.3 Comparison of ANSYS and ISLAB2000 with Ioannides “Equivalent” Plate Method

As mentioned in the previous section an “equivalent” plate may be used to represent a composite AC/PCC pavement in which the properties of the plate are based on the properties of the composite structure. The equivalent stresses with in the plate can then be used to determine the maximum displacement and stresses with in the layers of the composite AC/PCC pavement. Finite element analysis was used to verify this statement. In order to minimize the amount of work for calculations and the finite element analysis, the following properties were used; mesh size = 6 in x 6 in, $E_{PCC \text{ Overlay}} = 3,823,680$ psi, $E_{AC} = 1,354,680$ psi, $E_{PCC} = 3,100,000$ psi, $k_S = 150$ pci, $E_S = 3,970$ psi and $\nu_S = 0.40$. Also, a 9 kip load was distributed over a 144 sq. in. area located in the center of the slab.

5.3.1 Evaluation of Westergaard’s Equations for an Unbonded AC/PCC Pavement

In this work Westergaard’s equations for deflection and stress were chosen to determine the behavior of the “equivalent” plate. Finite element analyses were performed to verify Westergaard’s equations. Using properties and methods described in previous sections the thickness for the “equivalent” plate was determined to be 9.69 inches. A summary of the results are shown in Table 5-3. Calculations, deflection, and stress contours for the ISLAB2000 model can be seen in Appendix D.

Table 5-3 Summary of the “Equivalent” Plate Verification

| | Westergaard | ISLAB2000 (2-D) | ANSYS (3-D) | | |
|---------------------------------|-------------|-----------------|---------------|----------------------|--------------------------|
| | | | Shell Element | Single Solid Element | 2 Layered Solid Elements |
| Displacement (in) | 0.0083 | 0.0085 | 0.0035 | 0.0090 | 0.0089 |
| Stress (σ_{top} psi) | -133 | -138 | -131 | -125 | -128 |
| Stress (σ_{bottom} psi) | 133 | 138 | 131 | 120 | 107 |

The results showed that Westergaard’s equations are a valid method for determining the stresses and deflection in a homogeneous plate of uniform thickness. The 2-D analysis resulted in deflections with less than a one percent difference. However the stresses were 3% higher than Westergaard’s results. Of the 3-D analyses, use of shell elements produced the least amount of discrepancy in the stress distribution, but there was a 58% difference in the amount of deflection when compared to Westergaard. Also, when compared to Westergaard, the use of two layered elements produced a 7% difference in deflection and a 19% difference in the averaged stress distribution.

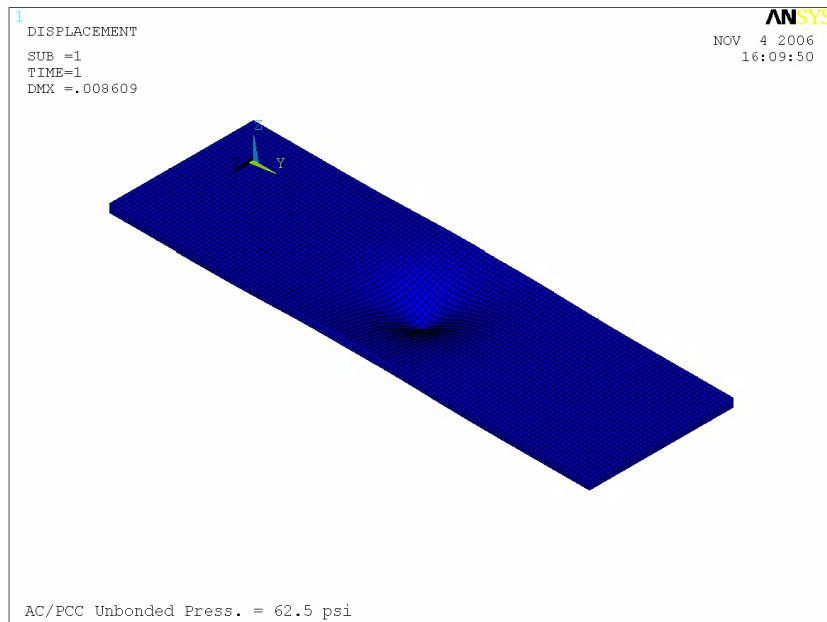
5.3.2 Application of the “Equivalent” Plate Method to an AC/PCC Pavement

Using Ioannides “equivalent” plate methodology as described in section 5.2.1, displacement and stresses in the top and bottom of each layer are determined for both an unbonded and bonded AC/PCC pavement [5]. Calculations for the Ioannides method are shown in Appendix E. These results were then compared to deflections and stresses determined from finite element analyses. A summary of the deflections for the unbonded AC/PCC pavement can be seen in Table 5-4.

Table 5-4 Summary of Displacements in the Unbonded AC/PCC Pavement

| | ISLAB2000 | ANSYS: PLATE Elements | ANSYS: SOLID Elements | Ioannides |
|-------------------|-----------|--------------------------|--------------------------|-----------|
| Displacement (in) | 0.0088 | n/a | 0.0086 | 0.0083 |

When compared to Ioannides the deflection results showed that ISLAB2000 produced a difference of 6%. ANSYS resulted in only a 4% difference when compared to Ioannides method. A graphical output from the ANSYS program, seen in Figure 5-1 shows an example of the deflection.

**Figure 5-1 Deflection of the Unbonded AC/PCC Pavement**

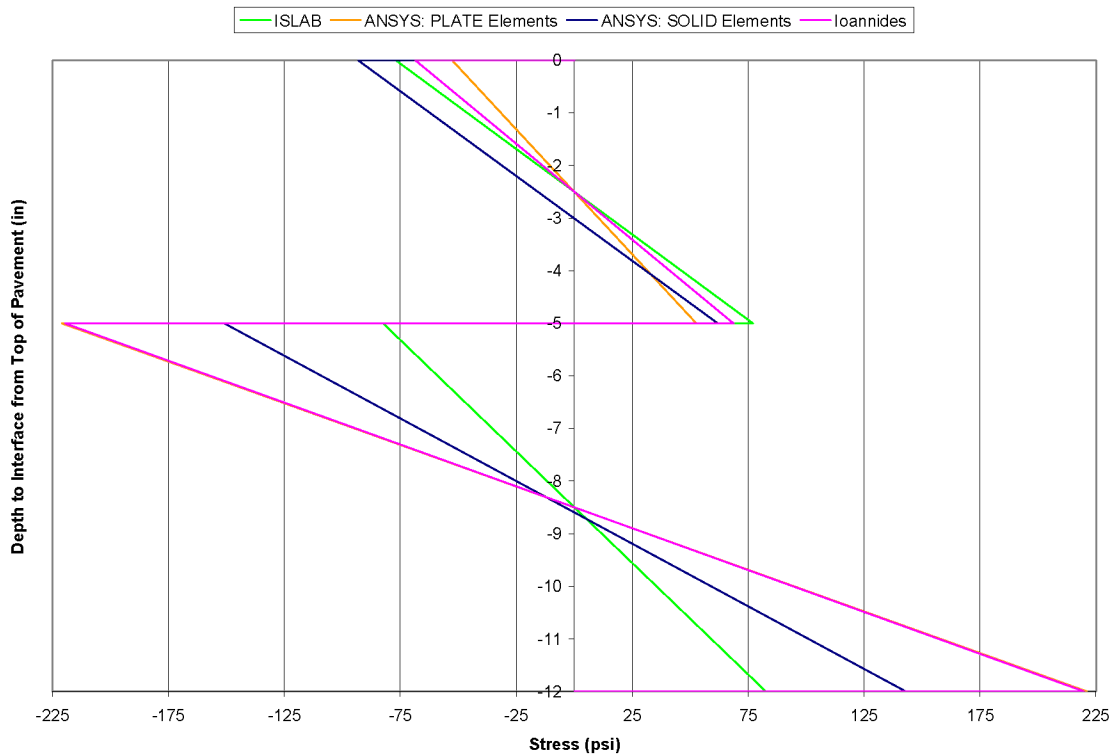


Figure 5-2 Summary of Stress Distributions in the Unbonded AC/PCC Pavement

Figure 5-2 shows the resulting stress distribution for the unbonded AC/PCC pavement. The 2-D model using ISLAB2000 produced 62% lower stresses for the PCC layer when compared to Ioannides solution. When comparing Ioannides results to the ISLAB2000 model, the Ioannides method produced 12% lower stresses in the top AC layer. The 3-D model using a layer of plate elements to model each consecutive layer produced a 1% difference in stress for the PCC layer when compared to Ioannides solution. However, the actual behavior of a pavement is more closely resembled by that of the solid element model. When comparing Ioannides results to the solid element model, the Ioannides method produced 30-35% higher stresses in the top of the AC layer and in the PCC layer.

Table 5-5 Summary of Displacements in the Bonded AC/PCC Pavement

| | ISLAB | ANSYS: SOLID Elements | Ioannides |
|-------------------|--------|-----------------------|-----------|
| Displacement (in) | 0.0053 | 0.0052 | 0.005 |

For the bonded case in Table 5-5, the deflection results showed that ISLAB2000 produced a difference of 6% when compared to Ioannides. ANSYS resulted in only a 4% difference when compared to Ioannides method.

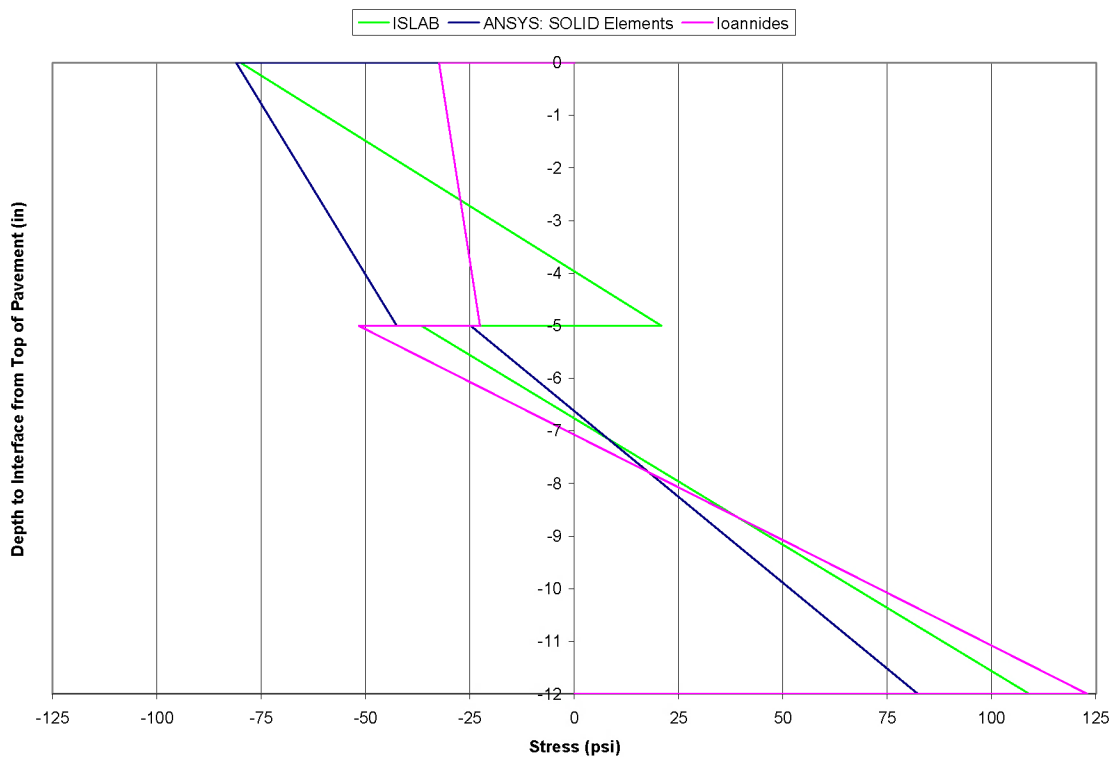


Figure 5-3 Summary of Stress Distributions in the Bonded AC/PCC Pavement

Figure 5-3 shows the resulting stress distributions for the bonded AC/PCC Pavement. The 2-D model using ISLAB2000, produced a range of 11-29% difference in stress for the PCC layer when compared to Ioannides solution. When comparing Ioannides results to the ISLAB2000 model, the Ioannides method produced 59% lower stresses in the top AC layer. The 3-D model using solid elements to model each consecutive layer produced 33% lower

stresses in the bottom of the PCC layer and 52% lower stresses for the top of the PCC layer when compared to Ioannides solution. The Ioannides method produced 60% lower stresses in the top AC layer when compared to the solid element model.

5.3.3 Application of the “Equivalent” Plate Method to a PCC/AC/PCC Pavement

Using the methodologies outlined in section 5.2.1 and applying the assumptions given in section 2.5.1 a “equivalent” plate solution for a PCC overlaid AC/PCC pavement was developed. For the calculations of the “equivalent” thickness for both the unbonded and bonded interface conditions it was assumed that the properties in the equivalent plate were equivalent to the properties of the PCC Overlay. The resulting equations and calculations are shown in Appendix F. The 2-D finite element program did not allow for the modeling of the three layered pavement. Therefore, only 3-D finite element analyses were performed to investigate the results of the modified Ioannides method.

Table 5-6 Summary of Displacements in the Unbonded PCC/AC/PCC Pavement

| | ISLAB | ANSYS: SOLID Elements | Ioannides |
|-------------------|-------|-----------------------|-----------|
| Displacement (in) | n/a | 0.0073 | 0.0077 |

Table 5-6 shows the deflections determined by the Ioannides method and ANSYS. When compared to Ioannides the deflection results showed that ANSYS produced only a 6%. The resulting stress distributions can be seen in Figure 5-4.

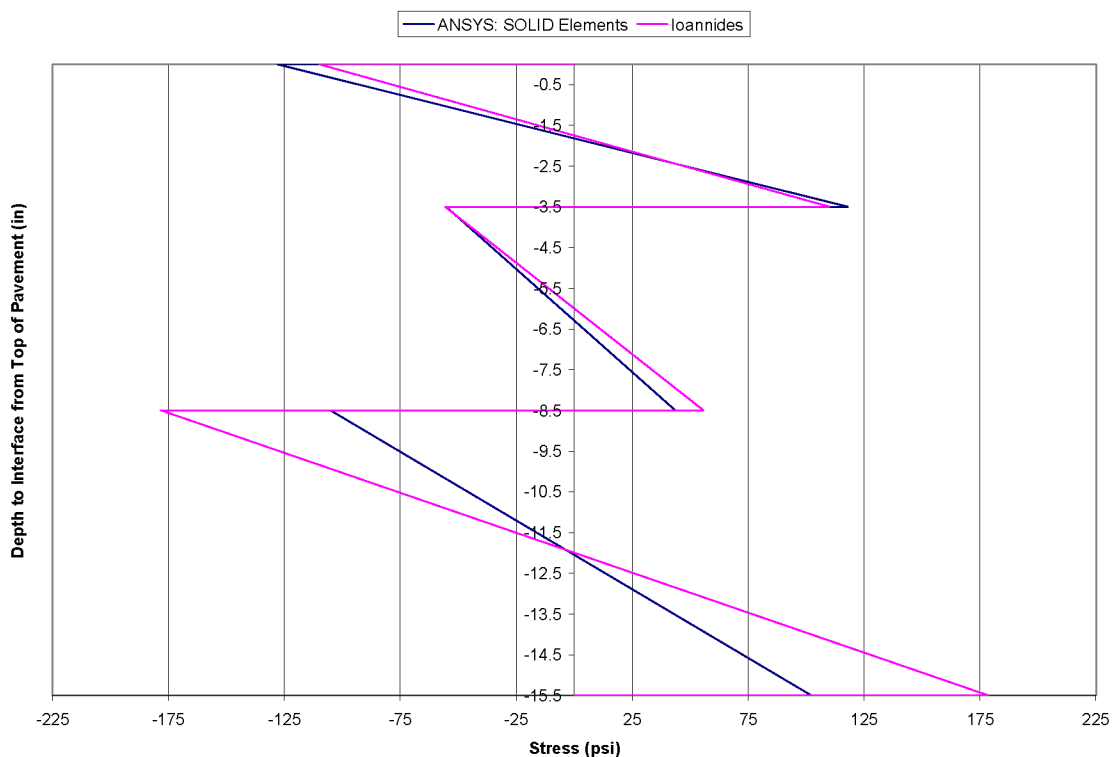


Figure 5-4 Summary of Stress Distributions in the Unbonded PCC/AC/PCC Pavement

Figure 5-2 shows the resulting stress distribution for the unbonded PCC/AC/PCC pavement. The 3-D model using ANSYS, produced 16% higher stresses for the PCC overlay when compared to Ioannides solution. When comparing Ioannides results to the ANSYS model, the Ioannides method produced 22% higher stresses in the bottom of the AC layer. The 3-D model produced a 40% difference in stresses for the lower PCC layer when compared to Ioannides solution.

Table 5-7 Summary of Displacements in the Bonded PCC/AC/PCC Pavement

| | ISLAB | ANSYS: SOLID Elements | Ioannides |
|-------------------|-------|-----------------------|-----------|
| Displacement (in) | n/a | 0.0028 | 0.0028 |

Table 5-7 shows the deflections determined by the Ioannides method and ANSYS. When compared to Ioannides the deflection results showed that ANSYS produced only a 1%. The resulting stress distributions can be seen in Figure 5-5.

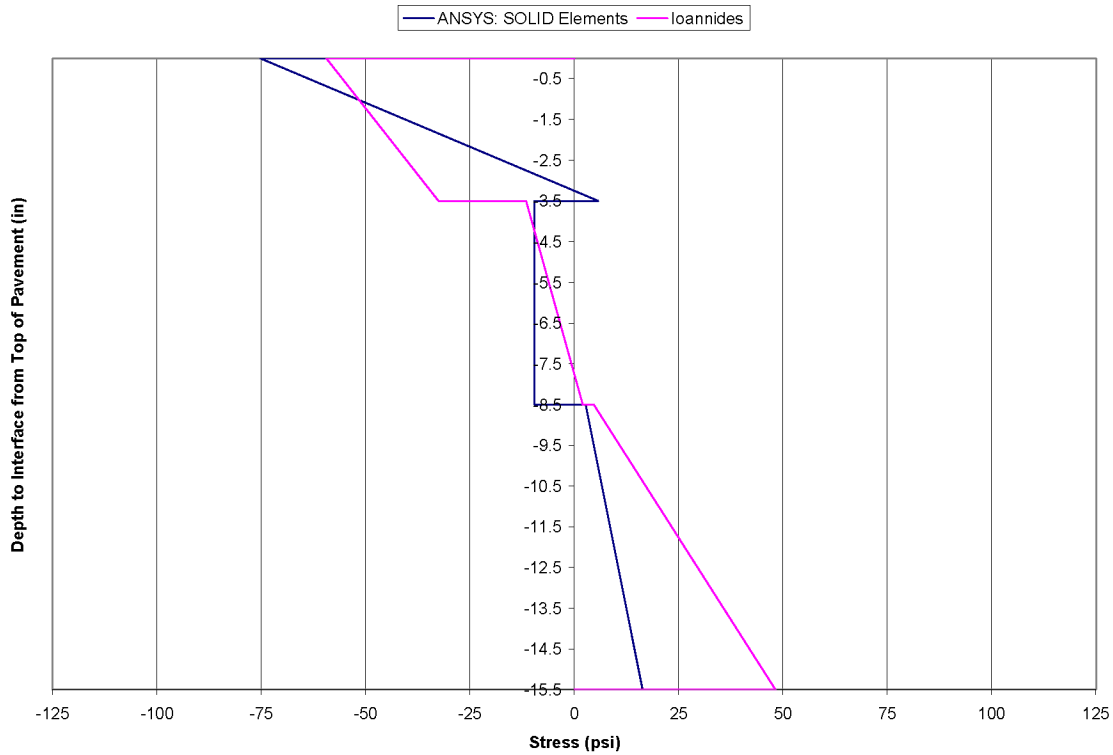


Figure 5-5 Summary of Stress Distributions in the Bonded PCC/AC/PCC Pavement

Figure 5-5 shows the resulting stress distribution for the bonded PCC/AC/PCC pavement. The 3-D model using ANSYS, produced 26% higher stresses for the top of the PCC overlay when compared to Ioannides solution. When comparing Ioannides results to the ANSYS model, the Ioannides method produced 17% higher stresses in the top of the AC layer. The 3-D model produced a 66% difference in stresses in the bottom of the lower PCC layer when compared to Ioannides solution.

6.0 SUMMARY, CONCLUSION, AND RECOMMENDATIONS

6.1 Summary

Iowa is one of few states with a large number of PCC pavements. Many of these pavements have exceeded their design life and are in need of rehabilitation. One method of rehabilitation is the PCC overlay. In order to improve the design process of overlays many states such as Iowa and Colorado have sponsored research projects such as Iowa Highway 13.

The usage of PCC overlays results in a behavior that is uniquely different from all other pavements. The complex behavior of the composite pavement is difficult to evaluate and much effort has gone into developing guidelines in order to evaluate these pavements accurately. Many of these guidelines incorporate guidelines for typical pavement design of a single placed layer. One method was the application of an “equivalent” plate to represent the actual behavior of the composite structure. In addition to these methods finite element analysis has also become a useful tool in the design of PCC overlays.

In order to investigate how the single placed layer guidelines could be applied to a composite pavement system, finite element modeling was utilized. Solid and shell elements were used to construct the various pavement layers. In addition these elements were used to model the subgrade under the pavement.

To aid in the evaluation of Iowa Highway 13 field investigation were performed. As part of the field investigation visual distress surveys and deflection data collection was performed to assess the condition of the pavement. Soils boring were also conducted to confirm the soil classification of the USDA soil survey.

Before the finite element modeling could be performed properties of the individual pavement layers and soil were calculated using AI's equation for the AC modulus and the backcalculation method developed by Hall and Darter [4]. The properties were input into the

finite element programs for analysis and used to calculate an “equivalent” thickness for the representative plate of the composite pavement. Stresses calculated for the “equivalent” plate were then used to backcalculate stresses in the individual layers of the two composite structures. The closed form solutions were then compared to the results from the finite element analysis.

6.2 Conclusions

The following are some conclusions made during analysis of the composite pavement on Iowa Highway 13:

- The backcalculation procedure developed by Hall and Darter for determining pavement properties is an acceptable method for the determination of soil modulus of subgrade reaction
- Westergaard’s equation are a valid method for determining stresses and deflections of pavement slab of uniform properties and thickness
- Deflections determined by finite element analysis for the composite pavements coincide with deflections calculated for their respective “equivalent” plate
- Composite pavements with fully bonded layer experience lower stresses and deflections than composite pavements whose layers are unbonded which verifies already established conclusions

6.3 Future Research Recommendations

The following are recommendations for future study:

- Further investigation into discrepancies between the different methods used to determine the stress distribution of the composite pavement
- Finite element analysis using variable element sizes and types to determine their effects on the resulting stress distribution

- Geometry of the loaded area, how much discrepancy is there between load distribution over a square area such as that used in finite element analysis versus distribution over a circular area assumed by Westergaard
- Development of more precise methods to determine materials properties of the soil such as the elastic modulus and poisson's ratio.

APPENDIX A

Table A-1 Northbound Lane Preconstruction FWD Data (Performed on 5/21/2002 on Previous Existing AC Roadway Surface)

| TS # | Lane | Station | Load (kip) | Sensor Number / Location | | | | | | | | | Pav't Temp |
|------|------|---------|------------|--------------------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------------|
| | | | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | |
| | | | | d ₀ | d ₈ | d ₁₂ | d ₁₈ | d ₂₄ | d ₃₆ | d ₄₈ | d ₆₀ | d ₁₂ | |
| 1 | NB | 43+02 | 9.06 | 4.75 | 3.91 | 3.67 | 3.49 | 3.25 | 2.76 | 2.3 | 1.79 | 3.56 | 53.1 |
| 2 | NB | 52+94 | 9.17 | 5.53 | 5.43 | 5.25 | 4.99 | 4.68 | 4.05 | 3.41 | 2.79 | 4.99 | 53.5 |
| 3 | NB | 63+03 | 9.06 | 6.59 | 5.74 | 5.4 | 4.96 | 4.51 | 3.62 | 2.87 | 2.21 | 5.75 | 53.8 |
| 4 | NB | 73+08 | 9 | 7.55 | 7.41 | 7.24 | 6.92 | 6.52 | 5.6 | 4.66 | 3.75 | 7.21 | 53.5 |
| 5 | NB | 83+13 | 8.89 | 7.43 | 7.31 | 7.29 | 7.18 | 7.05 | 5.57 | 4.32 | 3.24 | 6.64 | 54.2 |
| 6 | NB | 93+00 | 8.79 | 10.52 | 9.53 | 9.21 | 8.66 | 8.26 | 7.12 | 5.85 | 4.45 | 9.3 | 53.5 |
| 7 | NB | 103+09 | 8.65 | 7.52 | 7.13 | 6.79 | 6.29 | 5.86 | 4.84 | 3.9 | 3.31 | 5.94 | 54.6 |
| 8 | NB | 113+27 | 8.97 | 6.39 | 5.97 | 5.86 | 5.61 | 5.34 | 4.67 | 3.95 | 3.28 | 5.77 | 54.2 |
| 9 | NB | 123+09 | 8.78 | 6.65 | 6.36 | 6.23 | 5.91 | 5.58 | 4.81 | 4.01 | 3.26 | 5.96 | 54.2 |
| 10 | NB | 133+03 | 8.8 | 3.78 | 3.66 | 3.58 | 3.44 | 3.3 | 2.99 | 2.69 | 1.71 | 3.29 | 53.8 |
| 11 | NB | 143+00 | 8.81 | 3.37 | 3.13 | 2.96 | 2.81 | 2.69 | 2.38 | 2.07 | 1.77 | 2.88 | 52.4 |
| 12 | NB | 152+80 | 8.83 | 6 | 5.24 | 5.06 | 4.89 | 4.65 | 4.06 | 3.45 | 2.85 | 5.01 | 55.7 |
| 13 | NB | 163+02 | 8.78 | 7 | 6.6 | 6.3 | 5.96 | 5.38 | 4.57 | 3.79 | 3.09 | 5.47 | 55.7 |
| 14 | NB | 173+12 | 8.8 | 6.71 | 5.79 | 5.41 | 5.04 | 4.71 | 3.85 | 3.15 | 2.44 | 5.32 | 54.6 |
| 15 | NB | 186+22 | 8.94 | 7.04 | 6.03 | 5.71 | 5.37 | 5.01 | 4.19 | 3.35 | 2.61 | 5.8 | 55.3 |
| 16 | NB | 195+10 | 8.9 | 7.4 | 6.24 | 5.78 | 5.38 | 4.97 | 4.11 | 3.26 | 2.56 | 6.24 | 55.7 |
| 17 | NB | 205+12 | 8.34 | 7.2 | 6.91 | 6.59 | 6.16 | 5.63 | 4.57 | 3.63 | 2.8 | 5.83 | 54.6 |
| 18 | NB | 215+22 | 8.51 | 7.92 | 7.27 | 7.09 | 6.78 | 6.35 | 5.38 | 4.42 | 3.48 | 6.99 | 54.2 |
| 19 | NB | 225+34 | 8.35 | 6 | 5.85 | 5.8 | 5.59 | 5.17 | 4.28 | 3.48 | 2.77 | 5.41 | 56 |
| 20 | NB | 235+41 | 8.46 | 7.43 | 6.93 | 6.67 | 6.28 | 5.87 | 5.01 | 4.2 | 3.51 | 7.64 | 57.1 |
| 21 | NB | 245+64 | 8.4 | 5.53 | 5.2 | 5.11 | 4.91 | 4.66 | 4.03 | 3.38 | 2.71 | 4.9 | 56.4 |
| 22 | NB | 255+59 | 8.33 | 6.29 | 5.69 | 5.22 | 4.55 | 3.94 | 2.85 | 2.07 | 1.61 | 5.07 | 54.6 |
| 23 | NB | 268+29 | 8.03 | 10.3 | 10.18 | 10.13 | 10.06 | 9.95 | 6.59 | 5.48 | 4.43 | 9.29 | 56.8 |
| 24 | NB | 278+47 | 8.41 | 8.3 | 8.21 | 8.12 | 7.94 | 7.72 | 6.68 | 5.4 | 4.19 | 7.64 | 55.7 |
| 25 | NB | 289+31 | 8.48 | 6.88 | 6.32 | 6.06 | 5.83 | 5.58 | 4.93 | 4.25 | 3.52 | 6.01 | 56 |
| 26 | NB | 298+06 | 8.47 | 6.61 | 6.56 | 6.54 | 6.46 | 6.39 | 5.79 | 4.85 | 3.97 | 6.18 | 54.9 |
| 27 | NB | 308+11 | 8.53 | 6.75 | 6.13 | 5.9 | 5.69 | 5.46 | 4.87 | 4.3 | 3.69 | 6.04 | 55.7 |
| 28 | NB | 328+10 | 8.24 | 8.4 | 7.73 | 7.35 | 7.01 | 6.71 | 6.11 | 5.43 | 4.78 | 7.03 | 55.3 |
| 29 | NB | 328+17 | 8.36 | 7.94 | 6.99 | 6.64 | 6.3 | 5.98 | 5.32 | 4.48 | 3.73 | 6.61 | 55.3 |
| 30 | NB | 338+19 | 8.48 | 8.64 | 7.84 | 7.44 | 7.1 | 6.85 | 6.17 | 5.29 | 4.48 | 7.27 | 55.7 |
| 31 | NB | 348+23 | 8.4 | 11.05 | 10.35 | 10.18 | 9.93 | 9.62 | 8.87 | 7.95 | 7.05 | 10.34 | 51.6 |
| 32 | NB | 358+32 | 8.22 | 8.96 | 8.12 | 7.84 | 7.53 | 7.19 | 6.32 | 5.42 | 4.47 | 7.82 | 55.3 |
| 33 | NB | 368+44 | 8.3 | 8.47 | 7.22 | 6.78 | 6.4 | 6.03 | 5.25 | 4.44 | 3.61 | 7.11 | 52.7 |
| 34 | NB | 377+94 | 8.35 | 13.32 | 11.54 | 10.97 | 10.45 | 9.98 | 8.88 | 7.72 | 6.56 | 11.58 | 51.6 |
| 35 | NB | 388+04 | 8.36 | 9.06 | 7.64 | 7.16 | 6.68 | 6.22 | 5.27 | 4.41 | 3.63 | 7.96 | 56 |
| 36 | NB | 398+59 | 8.31 | 7.45 | 6.55 | 6.12 | 5.71 | 5.37 | 4.66 | 3.97 | 3.32 | 6.25 | 56.4 |
| 37 | NB | 408+09 | 8.25 | 5.63 | 5.11 | 4.96 | 4.82 | 4.59 | 4.03 | 3.4 | 2.85 | 4.85 | 56 |
| 38 | NB | 417+89 | 7.89 | 5.47 | 5.59 | 5.26 | 4.94 | 4.5 | 3.59 | 2.74 | 2.22 | 4.46 | 56.4 |
| 38 | NB | 419+49 | 8.39 | 13.51 | 11.06 | 9.38 | 7.65 | 6.27 | 4.29 | 3.1 | 2.23 | 9.9 | 55.7 |
| 39 | NB | 428+02 | 8.37 | 7.64 | 6.96 | 6.76 | 6.55 | 6.3 | 5.63 | 4.9 | 4.24 | 6.71 | 56 |
| 40 | NB | 437+08 | 8.12 | 12.11 | 11.23 | 10.83 | 10.26 | 9.69 | 8.43 | 7.27 | 6.19 | 12.25 | 56.8 |
| 41 | NB | 447+90 | 8.34 | 8.47 | 7.64 | 7.22 | 6.77 | 6.34 | 5.44 | 4.52 | 3.61 | 8.25 | 56 |
| 42 | NB | 459+03 | 8.11 | 10.02 | 9.04 | 8.7 | 8.35 | 7.96 | 7.06 | 6.13 | 5.17 | 9.2 | 54.6 |
| 43 | NB | 465+36 | 8.41 | 9.43 | 8.39 | 7.82 | 7.31 | 6.91 | 6.02 | 5.1 | 4.26 | 8.22 | 57.9 |
| 44 | NB | 475+02 | 8.18 | 6.28 | 6.1 | 5.92 | 5.74 | 5.54 | 5 | 4.4 | 3.74 | 5.8 | 59.7 |
| 45 | NB | 484+11 | 8 | 9.2 | 8.67 | 8.51 | 8.2 | 7.79 | 6.86 | 5.76 | 4.7 | 8.52 | 58.2 |
| 46 | NB | 491+10 | 8.12 | 7.79 | 7.34 | 7.19 | 6.9 | 6.55 | 5.66 | 4.72 | 3.81 | 6.93 | 58.2 |
| 47 | NB | 500+16 | 8.39 | 7.19 | 6.89 | 6.74 | 6.47 | 6.13 | 5.31 | 4.47 | 3.67 | 6.69 | 59.7 |
| 48 | NB | 508+19 | 8.35 | 5.15 | 5.01 | 4.89 | 4.67 | 4.43 | 3.85 | 3.26 | 2.7 | 4.9 | 59.7 |
| 49 | NB | 517+42 | 8.23 | 8 | 7 | 6.33 | 5.4 | 4.57 | 3.18 | 2.18 | 1.8 | 7.06 | 56.4 |
| 50 | NB | 518+92 | 8.24 | 6.03 | 5.36 | 4.93 | 4.35 | 3.82 | 2.84 | 2.09 | 1.69 | 4.74 | 57.9 |

Table A-2 Southbound Lane Preconstruction FWD Data (Performed on 5/21/2002 on Previous Existing AC Roadway Surface)

| TS # | Lane | Station | Load (kip) | Sensor Number / Location | | | | | | | | | Pav't Temp |
|------|------|---------|------------|--------------------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|------------|
| | | | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | |
| | | | | d ₀ | d ₈ | d ₁₂ | d ₁₈ | d ₂₄ | d ₃₆ | d ₄₈ | d ₆₀ | d ₁₂ | |
| 1 | SB | 525+02 | 8.18 | 6.15 | 5.6 | 5.17 | 4.57 | 4 | 2.91 | 2.07 | 1.66 | 4.89 | 58.2 |
| 2 | SB | 508+30 | 8.39 | 8.57 | 7.95 | 7.68 | 7.25 | 6.75 | 5.73 | 4.77 | 3.86 | 8.48 | 58.2 |
| 3 | SB | 498+74 | 8.56 | 9.34 | 8.69 | 8.46 | 8.05 | 7.64 | 6.66 | 5.65 | 4.7 | 8.86 | 57.9 |
| 4 | SB | 489+67 | 8.33 | 8.39 | 7.92 | 7.63 | 7.34 | 7.03 | 6.18 | 5.13 | 2.55 | 7.37 | 57.1 |
| 5 | SB | 480+01 | 8.04 | 6.41 | 5.8 | 5.61 | 5.46 | 5.26 | 4.73 | 4.11 | 3.47 | 5.34 | 58.2 |
| 6 | SB | 470+04 | 8.24 | 7.3 | 6.36 | 5.9 | 5.41 | 4.99 | 4.11 | 3.28 | 2.5 | 6.11 | 58.6 |
| 7 | SB | 462+84 | 8.28 | 8.54 | 7.45 | 7.12 | 6.88 | 6.58 | 5.81 | 5.05 | 4.27 | 7.28 | 58.6 |
| 8 | SB | 450+85 | 8.01 | 6.9 | 6.22 | 5.8 | 5.44 | 5.21 | 4.71 | 4.03 | 3.45 | 5.61 | 57.5 |
| 9 | SB | 441+05 | 8.41 | 9.51 | 9.04 | 8.9 | 8.62 | 8.29 | 7.4 | 6.46 | 5.44 | 8.91 | 58.6 |
| 10 | SB | 431+08 | 8.19 | 7.36 | 6.84 | 6.34 | 5.98 | 5.71 | 5.11 | 4.47 | 3.78 | 5.95 | 60.1 |
| 11 | SB | 420+99 | 8.45 | 6.85 | 6.24 | 6.04 | 5.78 | 5.48 | 4.73 | 3.97 | 3.22 | 6.22 | 59.7 |
| 12 | SB | 411+34 | 8.34 | 8.13 | 7.53 | 7.29 | 7.01 | 6.74 | 6.06 | 5.29 | 4.56 | 7.74 | 59.7 |
| 13 | SB | 401+13 | 8.53 | 6.73 | 5.91 | 5.67 | 5.44 | 5.16 | 4.51 | 3.82 | 3.22 | 5.73 | 58.6 |
| 14 | SB | 391+07 | 7.96 | 8.96 | 8.21 | 7.8 | 7.42 | 7.07 | 6.2 | 5.33 | 4.47 | 8.71 | 59.7 |
| 15 | SB | 381+43 | 8.31 | 7.84 | 7.37 | 7.23 | 6.99 | 6.7 | 5.98 | 5.19 | 4.39 | 7.26 | 59.7 |
| 16 | SB | 371+00 | 8.22 | 8.03 | 7.07 | 6.54 | 5.96 | 5.49 | 4.68 | 3.89 | 3.15 | 6.5 | 59.7 |
| 17 | SB | 360+76 | 8.14 | 7.64 | 7.37 | 6.78 | 6.31 | 5.9 | 4.92 | 4.02 | 3.22 | 6.34 | 59.7 |
| 18 | SB | 350+83 | 8.15 | 8.62 | 7.73 | 7.43 | 7.08 | 6.72 | 5.9 | 5.05 | 4.22 | 7.34 | 60.1 |
| 19 | SB | 340+67 | 8.51 | 8.61 | 8.18 | 8 | 7.74 | 7.48 | 6.75 | 5.91 | 5.09 | 8.14 | 59.7 |
| 20 | SB | 331+00 | 8.48 | 7.14 | 6.63 | 6.44 | 6.23 | 6.01 | 5.38 | 4.7 | 3.99 | 6.37 | 59.7 |
| 21 | SB | 321+05 | 8.09 | 8.24 | 7.65 | 7.53 | 7.35 | 7.1 | 6.38 | 5.56 | 4.74 | 7.43 | 59.3 |
| 22 | SB | 310+86 | 8.28 | 7.54 | 6.48 | 6.22 | 5.93 | 5.6 | 4.84 | 4.08 | 3.38 | 6.17 | 60.8 |
| 23 | SB | 300+87 | 8.11 | 9.04 | 8.75 | 8.59 | 8.27 | 7.91 | 7.03 | 5.97 | 4.57 | 8.63 | 59.7 |
| 24 | SB | 291+14 | 8.31 | 5.85 | 5.47 | 5.29 | 5.05 | 4.78 | 4.18 | 3.57 | 3 | 5.5 | 53.1 |
| 25 | SB | 279+94 | 8.01 | 9.45 | 8.65 | 8.26 | 7.91 | 7.42 | 6.37 | 5.33 | 4.33 | 7.78 | 63 |
| 26 | SB | 270+96 | 8.06 | 12.63 | 10.73 | 10.04 | 9.15 | 8.29 | 6.62 | 5.25 | 4.06 | 10.86 | 63 |
| 27 | SB | 260+26 | 8.03 | 7.14 | 6.42 | 5.89 | 5.18 | 4.54 | 3.38 | 2.5 | 2.09 | 7.01 | 60.4 |
| 28 | SB | 250+05 | 8.03 | 6.5 | 6 | 5.84 | 5.51 | 5.16 | 4.37 | 3.59 | 2.86 | 6.04 | 62.6 |
| 29 | SB | 240+08 | 8.36 | 5.63 | 5.42 | 5.31 | 5.1 | 4.73 | 3.83 | 3.05 | 2.34 | 5.09 | 62.6 |
| 30 | SB | 230+05 | 7.96 | 6.19 | 6.15 | 6.09 | 5.96 | 5.73 | 4.77 | 3.95 | 3.26 | 5.71 | 51.6 |
| 31 | SB | 219+35 | 8.14 | 8.56 | 8.49 | 8.49 | 8.35 | 7.66 | 6.14 | 4.85 | 3.7 | 7.2 | 64.8 |
| 32 | SB | 209+93 | 8.03 | 6.2 | 5.97 | 5.83 | 5.57 | 5.26 | 4.47 | 3.68 | 2.93 | 5.74 | 63.7 |
| 33 | SB | 199+95 | 8.26 | 7.51 | 5.8 | 5.03 | 4.52 | 4 | 3.09 | 2.39 | 1.77 | 4.92 | 65.2 |
| 34 | SB | 189+83 | 8.11 | 5.63 | 4.81 | 4.61 | 4.42 | 4.18 | 3.57 | 2.92 | 2.33 | 4.56 | 64.5 |
| 35 | SB | 175+90 | 8.11 | 6.21 | 6.05 | 5.94 | 5.74 | 5.49 | 4.93 | 4.37 | 2.26 | 5.88 | 63.4 |
| 36 | SB | 165+87 | 8.44 | 5.64 | 5.2 | 5.07 | 4.87 | 4.65 | 4.04 | 3.4 | 2.75 | 5.05 | 64.5 |
| 37 | SB | 155+59 | 7.92 | 3.48 | 3.28 | 3.18 | 3.04 | 2.92 | 2.69 | 2.5 | 2.37 | 3.02 | 64.5 |
| 38 | SB | 144+80 | 7.92 | 7.93 | 7.21 | 6.74 | 6.25 | 5.82 | 4.88 | 4.02 | 3.15 | 6.68 | 66.3 |
| 39 | SB | 136+24 | 8.34 | 5.61 | 4.96 | 4.81 | 4.64 | 4.44 | 3.9 | 3.36 | 2.76 | 4.59 | 63.4 |
| 40 | SB | 126+07 | 8 | 8.02 | 7.72 | 7.58 | 7.26 | 6.91 | 6.05 | 5.2 | 2.66 | 7.4 | 66.3 |
| 41 | SB | 116+26 | 8.07 | 6.19 | 6.05 | 5.91 | 5.67 | 5.35 | 4.56 | 3.77 | 3.03 | 5.76 | 67 |
| 42 | SB | 106+06 | 8.28 | 6.25 | 5.54 | 5.34 | 5.14 | 4.92 | 4.29 | 3.64 | 2.97 | 5.35 | 67.7 |
| 43 | SB | 95+29 | 8.11 | 6.24 | 6.16 | 6.01 | 5.83 | 5.6 | 4.95 | 4.23 | 3.48 | 5.6 | 66.7 |
| 44 | SB | 85+34 | 8.45 | 10.16 | 8.67 | 8.11 | 7.41 | 6.69 | 5.33 | 4.14 | 3.06 | 8.63 | 71.4 |
| 45 | SB | 75+41 | 8.17 | 6.75 | 6.1 | 5.9 | 5.62 | 5.3 | 4.51 | 3.72 | 3 | 6.15 | 71.8 |
| 46 | SB | 65+97 | 8.39 | 4.65 | 4.13 | 3.94 | 3.69 | 3.42 | 2.83 | 2.27 | 1.76 | 4.22 | 69.9 |
| 47 | SB | 55+95 | 8.4 | 8.45 | 7.77 | 7.29 | 6.59 | 5.89 | 4.55 | 3.31 | 2.11 | 6.97 | 70.7 |
| 48 | SB | 45+84 | 7.91 | 2.56 | 2.41 | 2.34 | 2.26 | 2.12 | 1.81 | 1.5 | 0 | 2.14 | 57.5 |

APPENDIX B

Table B-1 Soil Classification of Iowa Highway 13

| TS # | Stations | Soil Classification | | | | | | | | | |
|------|----------|---------------------|-------------|------------------------------|--|--|--------|-----------------------|---|--|-------------------------------------|
| | | USDA Classification | | | | | AASHTO | Visual Classification | | | |
| | | Stations | Soil Name | Sample Depth | USDA Texture | Unified | | Stations | Sample Depth / Size | Visual Description | Visual Classification (unified) |
| 9 | 52 to 56 | 51 to 63 | Waspie Loam | 0"-11" 11"-29" 29"-60" | Loam Loam, sandy loam, sandy clay Gravelly loamy sand, Gravelly sand, sand | CL, ML, CL-ML CL, SC, CL-ML, SM-SC SW, SM, SP, SP-SM | A-4 | 54+27 | 14"-20" 14"-40" 20"-40" 44"-56" 44"-74" 62"-74" 102"-122" | Top 6" dark brown sand with silt Brown to yellowish brown fine sand. Top 12" brown to yellowish brown fine sand. 6" gray sandy silty lenses Bottom 12" yellowish brown poorly graded sand. Yellowish orange to orangish brown well graded sand. | SM SP SP SP-SM SP SW |
| 11 | 57 to 61 | 51 to 63 | Waspie Loam | 0"-11" 11"-29" 29"-60" | Loam Loam, sandy loam, sandy clay Gravelly loamy sand, Gravelly sand, sand | CL, ML, CL-ML CL, SC, CL-ML, SM-SC SW, SM, SP, SP-SM | A-4 | 58+24 | 14"-40" 46"-75" 144"-166" | Brown to yellowish brown fine sand with silt. Yellowish orange well graded sand with some larger particles. Yellowish orange to orange yellow well graded sand with some larger particles. | SM SW SW |

| | | | | | | | | | | | | |
|----|-------------|----------------|-----------------------------|-------------|--|-------------------------|-------------|----------------------------|---------------|--|--|-----------|
| 15 | 67 to 71 | 68 to 72 | Lawler Loam | | | | A-6, A-7 | 68+50 | | | | |
| | | | | 0"- 17" | Loam | CL, ML | | | 12"-38" | Dark brown fine grained sand with yellowish orange well graded sand lenses with some fine gravel. | SW- SM | |
| | | | | 17"- 28" | Loam, sandy clay loam, clay loam | CL, SC | | | 72"-97" | Brown to yellowish brown well graded sand | SW | |
| | | | | 28"- 60 | Gravelly coarse sand, gravelly loamy sand, loamy coarse sand | SW, GP, SP, SW-SM | | | 107"- 117" | Yellowish brown well graded sand with some larger particles. | SW | |
| | | | | | | | | 107"- 135" Saturated | 117"- 125" | Yellowish brown clayey sand. | SC | |
| | | | | | | | | | 125"- 135" | Yellowish brown fine sand with few larger particles. | SP | |
| 21 | 82 to 86 | 80 to 84 | Clyde - Floyd Complex | | | | | | | | | |
| | | | Clyde | 0"- 23" | Clay loam | OL, MH, ML, OH | | 81+50 | 14"-24" | Dark brown sandy silt | CL | |
| | | | | 23"- 34" | Clay loam, loam, silty clay loam. | CL, ML | | | 14"-36" | 24"-26" | Yellowish/brown sandy clay | CL |
| | | | | 34"- 41" | Sandy loam, loam, sandy clay loam. | SM, SM-SC | | | | 26"-36" | Dark brown sandy silt | SC |
| | | | | 41"- 60" | Loam, sandy clay loam. | CL, SC | | | | 72"-101" | Yellowish/brown sandy clay with gray mottling | ML- CL |
| | | 84 to 92 | Floyd | 0"- 22" | Loam | OL, ML, CL | | | | 102"- 122" | Dark gray sandy clay, massive with some 1/2" particle | CL |
| | | | | 22"- 30" | Sandy clay loam, loam. | CL | A-6 | | | | | |

| | | | | | | | | | | |
|----|------------|------------|-------------|---------|-----------------------------------|-----------|----------|--------|---|----|
| | | | | 30"-36" | Sandy loam, loamy sand | SM, SM-SC | | | | |
| | | | | 36"-60" | Loam, clay loam, sandy clay loam. | CL | | | | |
| 23 | 87 to 91 | 84 to 92 | Kenyon Loam | 0"-17" | Loam | CL | A-6 | 88+50 | 12"-38" Yellowish/brown sandy clay with gray mottling at the top | CL |
| | | | | 17"-54" | Loam, clay loam, sandy clay loam. | CL | | | 41"-66" Yellowish/orange to brown sandy clay | CL |
| | | | | 54"-60" | Loam | CL | | | | |
| 31 | 107 to 113 | 101 to 117 | Kenyon Loam | 0"-17" | Loam | CL | A-6 | 108+55 | 48"-73" Yellowish/orange with gray mottling | CL |
| | | | | 17"-54" | Loam, clay loam, sandy clay loam. | CL | | | 116"-128" Yellowish/orange with gray mottling | CL |
| | | | | 54"-60" | Loam | CL | | | | |
| 36 | 125 to 129 | 121 to 153 | Kenyon Loam | 0"-17" | Loam | CL | A-6 | 126+80 | 18"-44" 18"-36" Yellowish/brown sandy-clay with light gray mottling | CL |
| | | | | 17"-54" | Loam, clay loam, sandy clay loam. | CL | | | 36"-44" Brown sandy-clay with 1/2" particles | CL |
| | | | | 54"-60" | Loam | CL | | | 56"-67" 56"-63" Gray-fine sand with clay | CL |
| | | | | | | | | | 63"-67" Brownish gray fine sand with silt and organic matter (roots) | CL |
| | | | | | | | | | 120" Bag sample Saturated gray sand with clay and yellow clay nodules | CL |
| 73 | 219 to 223 | 215 to | Olin Fine | | | | A-2, A-4 | 219+73 | | |

| | | | | | | | | | | |
|----|------------|------------|-----------------------|---------|------------------------------------|----------------|---------------------------|-----------|--|--------|
| | | 220 | Sandy Loam | 0"-28" | Fine sandy loam, sandy loam. | SM-SC, SC | | 13"-37" | Yellowish/brown sandy-clay with gray mottling and particle up to one inch | CL |
| | | | | 28"-46" | Loam, clay loam, sandy clay loam. | CL, SC | | 48"-72" | Yellowish/brown uniform in color sandy-clay | CL |
| | | | | 46'-60" | Loam, clay loam | CL | | 102"-121" | Brownish/gray clayey-sand, "massive", with particle up to one inch | CL |
| 75 | 224 to 228 | 220 to 229 | Clyde - Floyd Complex | | | | Clyde A-7, Floyd A-6, A-7 | | | |
| | | | Clyde | 0"-23" | Clay loam | OL, MH, ML, OH | | 226+48 | Low elevation potential fill material | |
| | | | | 23"-34" | Clay loam, loam, silty clay loam. | CL, ML | | 16"-43" | Dark brown fine to medium sand | CL, SC |
| | | | | 34"-41" | Sandy loam, loam, sandy clay loam. | SM, SM-SC | | 47"-53" | Brown sandy clay | SC |
| | | | | 41"-60" | Loam, sandy clay loam. | CL, SC | | 47"-70" | | |
| | | | | | | | | 53"-70" | Yellow clayey sandy | SC |
| | | | | | | | | 96"-? | Yellow sandy clay (Pinched tube) | SC |
| | | | | | | | | 124"-136" | Top-Yellow clay with some sand. Bottom-Fine yellowish/brown clayey sand with few 2" cobbles (possible parent material) | SC |
| | | | Floyd | 0"-22" | Loam | OL, ML, CL | | | | |
| | | | | 22"-30" | Sandy clay loam, loam. | CL | | | | |
| | | | | 30"-36" | Sandy loam, loamy sand | SM, SM-SC | | | | |

| | | | | | | | | | |
|----|---------------|------------------|--|--|---|---------------------------------------|--------------------|--|-------|
| | | | | Loam, clay loam, sandy clay loam. | CL | | | | |
| 79 | 234 to 238 | 232 to 262 | Clyde - Floyd Complex Clyde | | | Clyde A-7, Floyd A-6, A-7 | 234+50 | | |
| | | | | 0"- 23" | Clay loam | OL, MH, ML, OH | 12"-36" | Fine dark brown sand with yellow/orangish clay pockets (nodules). Less than 5% large aggregate approximately one inch. | ML |
| | | | | 23"- 34" | Clay loam, loam, silty clay loam. | CL, ML | 44"-53" | Dark brown medium to fine sand (homogeneous) | SM-SC |
| | | | | 34"- 41" | Sandy loam, loam, sandy clay loam. | SM, SM-SC | 44"-71" 53"-57" | Medium brown medium to fine sand (homogeneous) | SC |
| | | | | 41"- 60" | Loam, sandy clay loam. | CL,SC | 57"-71" | Dark brown medium to fine sand (homogeneous) | SC |
| | | | | 0"- 22" | Loam | OL, ML, CL | 96"-122" | Yellow medium to coarse sand | SW |
| | | | | 22"- 30" | Sandy clay loam, loam. | CL | | | |
| | | | Floyd | 30"- 36" | Sandy loam, loamy sand | SM, SM-SC | | | |
| | | | | 36"- 60" | Loam, clay loam, sandy clay loam. | CL | | | |
| 85 | 249 to 253 | 232 to 262 | Clyde - Floyd Complex | | | Clyde A-7, Floyd A-6, A-7 | 252+81 | | |

| | | | | | | | | | | |
|----|------------|------------|-------------|---------|------------------------------------|----------------|-----|--------------------|---|--------|
| | | | Clyde | | | | | | | |
| | | | | 0"-23" | Clay loam | OL, MH, ML, OH | | 12"-39" | Dark grayish/brown fine sand with large clay nodules gray in color | CL |
| | | | | 23"-34" | Clay loam, loam, silty clay loam. | CL, ML | | 72"-76" | Yellow sandy clay | CL |
| | | | | 34"-41" | Sandy loam, loam, sandy clay loam. | SM, SM-SC | | 72"-86" 76"-86" | Yellow clay with medium sand and gravel. Some mottling gray in color, possibly calcic | CL, SC |
| | | | | 41"-60" | Loam, sandy clay loam. | CL, SC | | 102"-113" | Yellow clay and very fine sand, bottom 1"-2" very fine cemented sand (possible bedrock or parent material) | CL, SC |
| | | | Floyd | 0"-22" | Loam | OL, ML, CL | | | | |
| | | | | 22"-30" | Sandy clay loam, loam. | CL | | | | |
| | | | | 30"-36" | Sandy loam, loamy sand | SM, SM-SC | | | | |
| | | | | 36"-60" | Loam, clay loam, sandy clay loam. | CL | | | | |
| 93 | 270 to 274 | 271 to 280 | Kenyon Loam | | | | A-6 | 275+22 | | |
| | | | | 0"-17" | Loam | CL | | 22"-47" | Light brown to yellowish brown, sandy lean clay with particle coatings, minor modeling (yellowish brown with gray patches). Fine gravel to coarse sand increasing with depth of sample. | CL |

| | | | | | | | | | | |
|----|------------|------------|-----------------------|--|----------------|-----|--|----------------|--|--------|
| | | | | Loam, clay loam, sandy clay loam. | CL | | | 67"-89" | Oxidized to unoxidized transition 10" from the top of the sample. Light yellowish brown to dark gray in color, well modeled with gravel up to 1 inch in size. Fractures present in the parent material which indicates coated oxidized flow paths. | CL |
| | | | | Loam | CL | | | 101"-125" | Dark gray stiff clay (unoxidized glacial till) below the water table. "Massive" Particle with a maximum size up to one inch. Very little sand. | CL |
| 98 | 280 to 284 | 280 to 283 | Clyde - Floyd Complex | | | | | | | |
| | | | Clyde | | | | | | | |
| | | | | Clay loam | OL, MH, ML, OH | | | 39" Bag sample | Yellowish/brown clean medium poorly graded sand | SP, SC |
| | | | | Clay loam, loam, silty clay loam. | CL, ML | | | 70"-95" | Yellowish/gray sandy clay with large gravel (2"-3") | CL, SC |
| | | | | Sandy loam, loam, sandy clay loam. | SM, SM-SC | | | | | |
| | | | | Loam, sandy clay loam. | CL, SC | | | | | |
| | | 283 to 287 | Floyd | Loam | OL, ML, CL | A-6 | | | | |
| | | | | Sandy clay loam, loam. | CL | | | | | |
| | | | | Sandy loam, loamy sand | SM, SM-SC | | | | | |

| | | | | | | | | | |
|-----|---------------|------------------|-------------------------|--|---|--|---------------|--|-----------|
| | | | | Loam, clay loam, sandy clay loam. | CL | | | | |
| 118 | 330 to 334 | 329 to 332 | Colo-Ely Complex | | | Colo A-4, A-6, Ely A-7, A-6 | 331+48 | | |
| | | | Colo | 0"- 18" | Silty loam | CL,CL- ML | 13"-16" | Medium brown fine sand | CL- ML |
| | | | | 18"- 47" | Silty clay loam | CL,CH | 16"-22" | Yellow brown to brown very clean sand | CL |
| | | | | 47"- 60" | Silty clay loam, clay loam, silt loam | CL,CH | 13"-37" | Dark brown sandy-silt to dark brown sandy clay towards the bottom | CL, ML |
| | | | Ely | 0"- 26" | Silty clay loam | CL, OH, MH | 66"-91" | Dark brown sandy-silt with lots of organic matter (possible fill material) | OH |
| | | | | 26"- 49" | Silty clay loam | CL, ML | 104"- 133" | Black/dark gray sandy-silt with lots of organic matter (possible top soil) | OH |
| | | | | 49"- 60" | silt loam, silty clay loam, loam. | CL | | | |
| 122 | 340 to 344 | 341 to 344 | Fayette Silt Loam | | | A-4, A-6 | 342+90 | | |
| | | | | 0"- 12" | Silt loam. | CL- ML, CL | 16"-28" | Yellowish/brown with mottling gray in color, blocky structure | CL,ML |
| | | | | 12"- 46" | Silty clay loam, clay loam | CL | 16"-41" | Dark brown clayey silt | CL- ML |
| | | | | 46"- 60" | Silt loam. | CL | 67"-75" | Dark brown clayey silt | CL- ML |
| | | | | | | | 67"-83" | Yellowish/brown with mottling gray in color, blocky structure | CL |
| | | | | | | | 102"- 127" | Light gray very fine sandy-silt with iron oxide staining | CL,ML |

| | | | | | | | | | | |
|-----|------------|------------|-----------------------|---------|------------------------------------|---------------------------|---------|----------|---|-------|
| 144 | 395 to 399 | 396 to 405 | Basset Loam | | | A-4, A-6 | 396+50 | | | |
| | | | | 0"-12" | Loam | CL, CL-ML | | 12"-26" | Yellowish/brown well graded sand | CL |
| | | | | 20"-42" | Loam, fine sandy loam. | CL | 12"-38" | 26"-38" | Yellowish/brown sandy-clay with gray mottling | CL-ML |
| | | | | 42"-60" | Loam | CL | | 42"-71" | Dark gray clay with sand and gravel, "massive" | CL |
| | | | | | | | | 96"-124" | Dark gray lean clay with sand. | CL |
| 164 | 445 to 449 | 431 to 457 | Clyde - Floyd Complex | | | Clyde A-7, Floyd A-6, A-7 | 448+50 | | | |
| | | | Clyde | 0"-23" | Clay loam | OL, MH, ML, OH | | 10"-31" | Light brown to yellowish/brown sandy-silt, "mottled" | ML |
| | | | | 23"-34" | Clay loam, loam, silty clay loam. | CL, ML | | 51"-75" | Light gray very fine sandy/silt with iron oxide staining | ML |
| | | | | 34"-41" | Sandy loam, loam, sandy clay loam. | SM, SM-SC | | 104"-? | Light gray to light brown sandy-silt with orangish sand seams | ML |
| | | | | 41"-60" | Loam, sandy clay loam. | CL, SC | | | | |
| | | | Floyd | 0"-22" | Loam | OL, ML, CL | | | | |
| | | | | 22"-30" | Sandy clay loam, loam. | CL | | | | |
| | | | | 30"-36" | Sandy loam, loamy sand | SM, SM-SC | | | | |
| | | | | 36"-60" | Loam, clay loam, sandy clay loam. | CL | | | | |
| 166 | 450 to 454 | 431 to 457 | Clyde - Floyd Complex | | | Clyde A-7, Floyd A-6, A-7 | 452+00 | | | |

| | | | | | | | | | | |
|-----|------------------|------------|-----------------------|---------|-----------------------------------|----------------|--|---------------------------|--|----|
| | | | Clyde | 0"-23" | Clay loam | OL, MH, ML, OH | | 12"-Rock | Yellowish/brown sandy silt with stiff platy structure | ML |
| | | | | 23"-34" | Clay loam, silty clay loam. | CL, ML | | 96" Bag sample | Yellowish/brown sandy silt with stiff platy structure | ML |
| | | | | 34"-41" | Sandy loam, sandy clay loam. | SM, SM-SC | | | | |
| | | | | 41"-60" | Loam, sandy clay loam. | CL, SC | | | | |
| | | | Floyd | 0"-22" | Loam | OL, ML, CL | | | | |
| | | | | 22"-30" | Sandy clay loam, loam. | CL | | | | |
| | | | | 30"-36" | Sandy loam, loamy sand | SM, SM-SC | | | | |
| | | | | 36"-60" | Loam, clay loam, sandy clay loam. | CL | | | | |
| 186 | 495+50 to 499+50 | 495 to 498 | Clyde - Floyd Complex | | | | | Clyde A-7, Floyd A-6, A-7 | | |
| | | | Clyde | 0"-23" | Clay loam | OL, MH, ML, OH | | 498+00 | | |
| | | | | 23"-34" | Clay loam, silty clay loam. | CL, ML | | 12"-Rock | 12"-25" Yellowish sandy clay with light gray mottling and gravel up to 3/4" | CL |
| | | | | 34"-41" | Sandy loam, sandy clay loam. | SM, SM-SC | | | 25"-27" Brownish/yellow sandy clay | SC |
| | | | | 41"-60" | Loam, sandy clay loam. | CL, SC | | 42"-66" | 42"-57" Dark brown fine to coarse sandy clay | CL |
| | | 498 to 504 | Floyd | 0"-22" | Loam | OL, ML, CL | | A-6 | 57"-66" Dark brown fine sandy clay with 2" seam of yellowish brown fine sand | CL |

| | | | | | | | | | |
|-----|------------------|------------|------------------------------------|--|----------------|-----|----------|--|----|
| | | | | 22"-30" Sandy clay loam, loam. | CL | | | 104"-129" Dark brown fine to coarse sandy clay | CL |
| | | | | 30"-36" Sandy loam, loamy sand | SM, SM-SC | | | | |
| | | | | 36"-60" Loam, clay loam, sandy clay loam. | CL | | | | |
| 189 | 500+50 to 506+50 | 504 to 507 | Clyde - Floyd Complex Clyde | 0"-23" Clay loam | OL, MH, ML, OH | | 501+50 | 12"-27" Medium brown fine sand | CL |
| | | | | 23"-34" Clay loam, silty clay loam. | CL, ML | | 12"-37" | 27"-29" Yellowish/brown sandy clay | CL |
| | | | | 34"-41" Sandy loam, sandy clay loam. | SM, SM-SC | | | 29"-37" Dark brown fine to medium sand with silt and grayish/green clay lenses | CL |
| | | | | 41"-60" Loam, sandy clay loam. | CL, SC | | | 44"-69" Dark brown/gray silty clay with organic material (possible fill material) | SC |
| | | | Floyd | 0"-22" Loam | OL, ML, CL | | 99"-122" | 99"-101" Brown medium sandy clay | CL |
| | | | | 22"-30" Sandy clay loam, loam. | CL | | | 101"-110" light yellowish/brown sandy clay with gray mottling | CL |
| | | | | 30"-36" Sandy loam, loamy sand | SM, SM-SC | | | 110"-122" Grayish sandy clay with gravel up to one inch | CL |
| | | | | 36"-60" Loam, clay loam, sandy clay loam. | CL | | | | |
| 191 | 507+60 | 507 | Kenyon | | | A-6 | 509+60 | | |

| | | | | | | | | | | |
|--|--------------|-----------|------|-------------|--|----|--|-------------------|--|----|
| | to 513+70 | to 510 | Loam | | | | | | | |
| | | | | 0"- 17" | Loam | CL | | 16"-42" | Dark brown medium sand with 2" yellow sand seam 10" from top | CL |
| | | | | 17"- 54" | Loam, clay loam, sandy clay loam. | CL | | 34"-40" | Dark brown clean sand | CL |
| | | | | 54"- 60" | Loam | CL | | 96" Bag sample | Yellow fine to medium sand, "saturated" | CL |

APPENDIX C

Table C-1 Iowa Highway 13 – Whitetopping Input Parameters

| Iowa Highway 13 - Whitetopping Input Parameters | | |
|---|----------------------|------------------------|
| <u>Existing Pavement Conditions</u> | | |
| Mean Monthly Air Temperature, °F | | 61 |
| Joint Spacing, in | | 108 |
| Thickness of the Asphalt Layer, in | | 5 |
| Poisson's Ratio of the Asphalt | | 0.35 |
| Thickness of the PCC Layer, in | | 7 |
| Poisson's Ratio of the PCC | | 0.15 |
| <u>Asphalt Layer's Mix Information</u> | | |
| Percent Aggregate Passing #200 Sieve | | 6 |
| Asphalt Content, Percent by Weight of Mix | | 5.5 |
| Percent Air Voids | | 4 |
| Original pen_{25} | | 90 |
| Aged pen_{25} | | 58.5 |
| η_{Aged} | | 3.92 |
| <u>Design Values</u> | | |
| Concrete Flexural Strength, psi | | 650 |
| Asphalt Elastic Modulus, psi | | 1354680 |
| | Bonded Conditions | Unbonded Conditions |
| Modulus of Subgrade Reaction, pci | 150 | 143 |
| PCC Elastic Modulus at 75% Cumulative, psi | 3100000 | 3700000 |
| Effective Thickness of Existing Pavement, in | 10.4 | 9.69 |

Table C-2 Backcalculation of Properties for Unbonded AC/PCC Pavement

| d_{PCC} (mils) | $AREA_{PCC}$ | Radius of Relative Stiffness, l | L/l_{est} | AF d_o | AF l | Adj d_{PCC} | Adj l | k-Value | E_{PCC} |
|---------------------|--------------|---|-------------|----------|--------|---------------|---------|---------|-----------|
| 3.91 | 33.378 | 61.281 | 1.762 | 0.637 | 0.705 | 2.657 | 43.184 | 225 | 26735656 |
| 8.48 | 28.319 | 27.868 | 3.875 | 0.869 | 0.926 | 7.597 | 25.819 | 217 | 3296409 |
| 7.18 | 31.999 | 45.702 | 2.363 | 0.732 | 0.813 | 5.444 | 37.139 | 148 | 9622304 |
| 8.22 | 32.888 | 54.536 | 1.980 | 0.675 | 0.752 | 5.729 | 40.989 | 116 | 11159612 |
| 12.09 | 29.032 | 30.115 | 3.586 | 0.851 | 0.914 | 10.505 | 27.511 | 138 | 2713016 |
| 8.39 | 32.112 | 46.656 | 2.315 | 0.726 | 0.806 | 6.275 | 37.610 | 125 | 8562488 |
| 7.39 | 31.555 | 42.354 | 2.550 | 0.756 | 0.835 | 5.781 | 35.381 | 153 | 8214035 |
| 7.75 | 32.794 | 53.421 | 2.022 | 0.682 | 0.759 | 5.463 | 40.565 | 124 | 11460076 |
| 7.02 | 33.318 | 60.349 | 1.790 | 0.642 | 0.711 | 4.674 | 42.918 | 129 | 15009880 |
| 5.38 | 31.290 | 40.592 | 2.661 | 0.768 | 0.847 | 4.335 | 34.388 | 216 | 10342104 |
| 8.34 | 29.769 | 32.863 | 3.286 | 0.828 | 0.897 | 7.121 | 29.477 | 178 | 4605059 |
| 6.39 | 31.499 | 41.966 | 2.573 | 0.758 | 0.838 | 5.046 | 35.167 | 178 | 9295639 |
| 7.40 | 29.816 | 33.057 | 3.267 | 0.827 | 0.896 | 6.333 | 29.611 | 199 | 5226191 |
| 8.03 | 30.926 | 38.413 | 2.812 | 0.785 | 0.862 | 6.504 | 33.096 | 155 | 6377404 |
| 7.83 | 28.225 | 27.598 | 3.913 | 0.871 | 0.928 | 7.052 | 25.611 | 237 | 3493146 |
| 9.11 | 27.359 | 25.328 | 4.264 | 0.890 | 0.940 | 8.345 | 23.817 | 231 | 2544815 |
| 8.97 | 31.726 | 43.581 | 2.478 | 0.747 | 0.827 | 6.890 | 36.045 | 124 | 7156130 |
| 8.89 | 33.406 | 61.711 | 1.750 | 0.635 | 0.702 | 5.811 | 43.302 | 102 | 12291940 |
| 9.33 | 32.626 | 51.567 | 2.094 | 0.694 | 0.772 | 6.653 | 39.821 | 105 | 9064358 |
| 6.80 | 32.508 | 50.341 | 2.145 | 0.701 | 0.781 | 4.956 | 39.302 | 145 | 11851528 |
| 8.17 | 28.907 | 29.696 | 3.637 | 0.854 | 0.916 | 7.198 | 27.202 | 207 | 3868906 |
| 11.49 | 31.082 | 39.314 | 2.747 | 0.778 | 0.856 | 9.140 | 33.639 | 107 | 4690674 |
| 13.16 | 30.010 | 33.878 | 3.188 | 0.820 | 0.891 | 11.000 | 30.174 | 110 | 3126131 |
| 10.20 | 30.858 | 38.030 | 2.840 | 0.788 | 0.864 | 8.240 | 32.861 | 124 | 4962332 |
| 8.39 | 33.739 | 67.600 | 1.598 | 0.605 | 0.661 | 5.232 | 44.683 | 107 | 14544115 |
| 10.10 | 32.349 | 48.786 | 2.214 | 0.711 | 0.791 | 7.368 | 38.612 | 101 | 7691383 |
| 10.26 | 30.250 | 34.956 | 3.090 | 0.811 | 0.884 | 8.539 | 30.896 | 136 | 4225297 |
| 10.56 | 31.129 | 39.594 | 2.728 | 0.776 | 0.854 | 8.394 | 33.805 | 116 | 5159000 |
| 9.94 | 31.352 | 40.992 | 2.635 | 0.765 | 0.845 | 7.811 | 34.618 | 118 | 5817474 |
| 13.11 | 32.826 | 53.803 | 2.007 | 0.680 | 0.757 | 9.089 | 40.712 | 74 | 6938691 |
| 11.49 | 30.646 | 36.899 | 2.927 | 0.796 | 0.871 | 9.357 | 32.155 | 114 | 4181300 |
| 10.79 | 29.274 | 30.965 | 3.488 | 0.844 | 0.908 | 9.323 | 28.131 | 149 | 3198973 |
| 14.63 | 28.789 | 29.309 | 3.685 | 0.857 | 0.918 | 12.765 | 26.913 | 119 | 2134820 |
| 10.81 | 29.881 | 33.327 | 3.241 | 0.824 | 0.894 | 9.129 | 29.797 | 136 | 3672245 |
| 10.69 | 29.808 | 33.024 | 3.270 | 0.827 | 0.896 | 9.050 | 29.588 | 139 | 3651421 |
| 7.82 | 30.758 | 37.485 | 2.881 | 0.792 | 0.868 | 6.397 | 32.523 | 164 | 6259709 |
| 8.75 | 32.006 | 45.762 | 2.360 | 0.732 | 0.812 | 6.596 | 37.170 | 122 | 7954909 |
| 13.12 | 24.897 | 20.515 | 5.264 | 0.930 | 0.964 | 12.441 | 19.771 | 223 | 1164727 |
| 9.58 | 31.062 | 39.199 | 2.755 | 0.779 | 0.856 | 7.666 | 33.570 | 128 | 5569567 |
| 14.09 | 31.762 | 43.850 | 2.463 | 0.745 | 0.825 | 10.689 | 36.188 | 79 | 4650299 |

Table C-2 (continued)

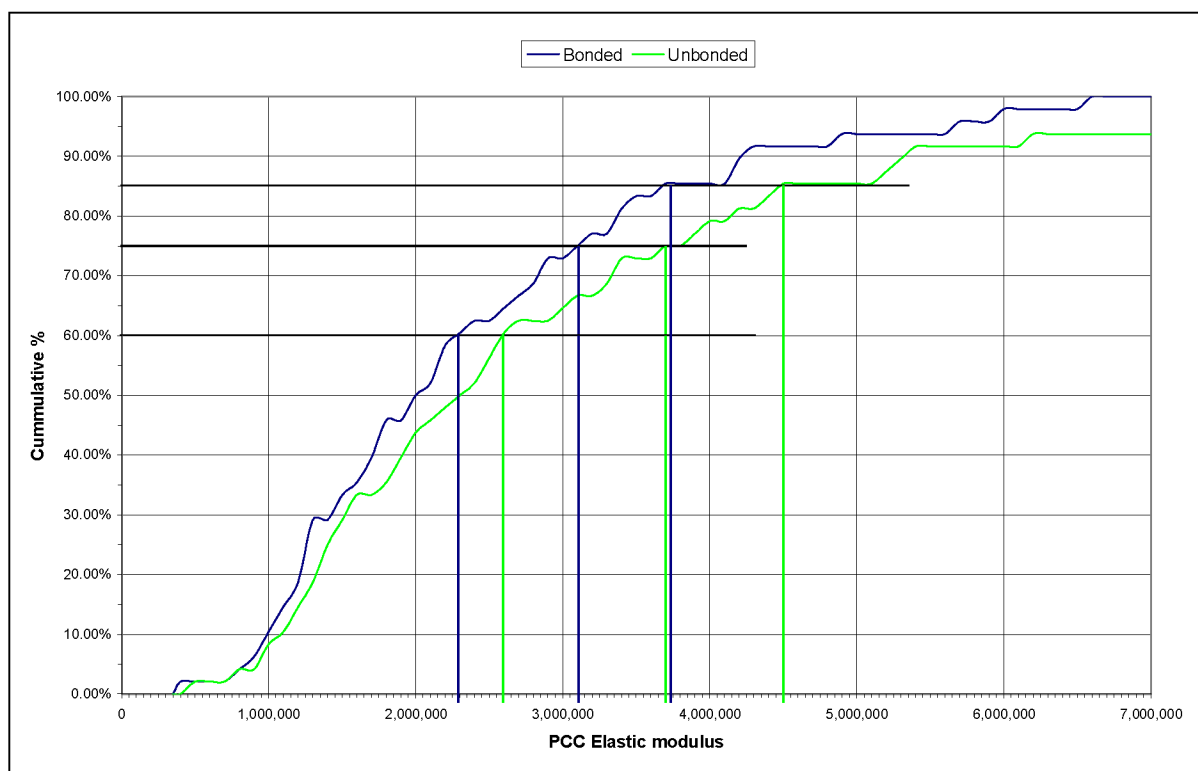
| | | | | | | | | | |
|-------|--------|--------|-------|-------|-------|--------|--------|-----|----------|
| 10.17 | 29.740 | 32.744 | 3.298 | 0.829 | 0.898 | 8.648 | 29.394 | 148 | 3770224 |
| 12.41 | 30.310 | 35.233 | 3.065 | 0.809 | 0.882 | 10.254 | 31.080 | 112 | 3561217 |
| 10.60 | 28.549 | 28.554 | 3.782 | 0.863 | 0.923 | 9.379 | 26.344 | 169 | 2781849 |
| 8.10 | 32.524 | 50.495 | 2.139 | 0.700 | 0.780 | 5.859 | 39.368 | 122 | 10057702 |
| 11.52 | 32.150 | 46.982 | 2.299 | 0.723 | 0.804 | 8.522 | 37.768 | 91 | 6359340 |
| 10.87 | 31.831 | 44.375 | 2.434 | 0.741 | 0.822 | 8.249 | 36.463 | 101 | 6118782 |
| 9.79 | 31.645 | 42.991 | 2.512 | 0.751 | 0.831 | 7.547 | 35.729 | 115 | 6417899 |
| 7.06 | 30.018 | 33.914 | 3.185 | 0.820 | 0.890 | 6.003 | 30.198 | 202 | 5738242 |

Table C-3 Backcalculation of Properties for Bonded AC/PCC Pavement

| d_{PCC} (mils) | $AREA_{PCC}$, in | Radius of Relative Stiffness, l | L/l_{est} | AF d_o | AF l | Adj d_{PCC} | Adj l | k- Value | E_{PCC} |
|---------------------|-------------------|---------------------------------------|-------------|----------|-------|---------------|--------|-------------|-----------|
| 4.04 | 32.507 | 50.326 | 2.146 | 0.701 | 0.781 | 2.925 | 39.295 | 246 | 20071262 |
| 8.61 | 27.986 | 26.930 | 4.010 | 0.877 | 0.932 | 7.665 | 25.091 | 227 | 3081716 |
| 7.30 | 31.541 | 42.258 | 2.556 | 0.756 | 0.836 | 5.624 | 35.328 | 158 | 8418663 |
| 8.35 | 32.474 | 49.997 | 2.160 | 0.704 | 0.783 | 5.968 | 39.152 | 122 | 9766170 |
| 12.22 | 28.790 | 29.311 | 3.685 | 0.857 | 0.918 | 10.587 | 26.915 | 143 | 2574506 |
| 8.52 | 31.718 | 43.524 | 2.481 | 0.747 | 0.827 | 6.463 | 36.015 | 132 | 7616906 |
| 7.52 | 31.118 | 39.532 | 2.732 | 0.776 | 0.854 | 5.940 | 33.768 | 164 | 7274491 |
| 7.88 | 32.356 | 48.852 | 2.211 | 0.711 | 0.791 | 5.694 | 38.642 | 131 | 9968407 |
| 7.15 | 32.827 | 53.806 | 2.007 | 0.680 | 0.757 | 4.948 | 40.713 | 136 | 12746761 |
| 5.51 | 30.700 | 37.178 | 2.905 | 0.794 | 0.870 | 4.480 | 32.331 | 236 | 8831146 |
| 8.47 | 29.408 | 31.457 | 3.433 | 0.839 | 0.906 | 7.220 | 28.485 | 188 | 4237073 |
| 6.52 | 30.996 | 38.814 | 2.783 | 0.782 | 0.859 | 5.201 | 33.339 | 192 | 8094570 |
| 7.53 | 29.410 | 31.462 | 3.433 | 0.839 | 0.905 | 6.432 | 28.489 | 211 | 4757002 |
| 8.16 | 30.533 | 36.321 | 2.973 | 0.801 | 0.875 | 6.638 | 31.787 | 165 | 5758470 |
| 7.96 | 27.866 | 26.610 | 4.059 | 0.880 | 0.933 | 7.118 | 24.840 | 250 | 3250911 |
| 9.24 | 27.062 | 24.633 | 4.384 | 0.896 | 0.944 | 8.399 | 23.253 | 241 | 2407331 |
| 9.09 | 31.363 | 41.059 | 2.630 | 0.765 | 0.844 | 7.058 | 34.656 | 131 | 6452419 |
| 9.02 | 33.015 | 56.121 | 1.924 | 0.666 | 0.741 | 6.097 | 41.561 | 106 | 10783664 |
| 9.46 | 32.265 | 48.000 | 2.250 | 0.717 | 0.797 | 6.874 | 38.250 | 110 | 8088858 |
| 6.93 | 32.017 | 45.852 | 2.355 | 0.731 | 0.812 | 5.165 | 37.215 | 155 | 10183666 |
| 8.30 | 28.552 | 28.566 | 3.781 | 0.863 | 0.923 | 7.277 | 26.353 | 218 | 3587591 |
| 11.62 | 30.804 | 37.737 | 2.862 | 0.790 | 0.866 | 9.280 | 32.680 | 112 | 4356824 |
| 13.28 | 29.778 | 32.899 | 3.283 | 0.828 | 0.897 | 11.106 | 29.502 | 114 | 2957979 |
| 10.33 | 30.548 | 36.396 | 2.967 | 0.800 | 0.875 | 8.371 | 31.835 | 130 | 4580083 |
| 8.52 | 33.321 | 60.387 | 1.788 | 0.642 | 0.711 | 5.555 | 42.929 | 109 | 12634151 |
| 10.22 | 32.018 | 45.862 | 2.355 | 0.731 | 0.812 | 7.570 | 37.219 | 106 | 6950015 |
| 10.39 | 29.950 | 33.621 | 3.212 | 0.822 | 0.892 | 8.651 | 29.998 | 142 | 3928189 |
| 10.69 | 30.826 | 37.858 | 2.853 | 0.789 | 0.865 | 8.536 | 32.755 | 121 | 4758940 |
| 10.07 | 31.029 | 39.002 | 2.769 | 0.780 | 0.858 | 7.961 | 33.452 | 124 | 5324775 |
| 13.24 | 32.566 | 50.930 | 2.121 | 0.698 | 0.777 | 9.326 | 39.554 | 76 | 6379165 |
| 11.62 | 30.374 | 35.538 | 3.039 | 0.807 | 0.880 | 9.482 | 31.280 | 119 | 3901748 |
| 10.92 | 29.000 | 30.008 | 3.599 | 0.851 | 0.914 | 9.409 | 27.432 | 155 | 3011086 |
| 14.76 | 28.590 | 28.683 | 3.765 | 0.862 | 0.922 | 12.843 | 26.441 | 122 | 2046894 |
| 10.94 | 29.601 | 32.191 | 3.355 | 0.834 | 0.901 | 9.230 | 29.006 | 142 | 3438589 |
| 10.81 | 29.525 | 31.899 | 3.386 | 0.836 | 0.903 | 9.150 | 28.800 | 145 | 3418808 |
| 7.95 | 30.357 | 35.459 | 3.046 | 0.807 | 0.881 | 6.524 | 31.227 | 174 | 5651810 |
| 8.88 | 31.630 | 42.880 | 2.519 | 0.752 | 0.832 | 6.777 | 35.669 | 129 | 7122640 |
| 13.25 | 24.714 | 20.228 | 5.339 | 0.932 | 0.965 | 12.471 | 19.519 | 228 | 1131598 |
| 9.71 | 30.730 | 37.340 | 2.892 | 0.793 | 0.869 | 7.805 | 32.433 | 135 | 5101387 |
| 14.22 | 31.529 | 42.177 | 2.561 | 0.757 | 0.837 | 10.859 | 35.283 | 82 | 4348601 |

Table C-3 (continued)

| | | | | | | | | | |
|-------|--------|--------|-------|-------|-------|--------|--------|-----|---------|
| 10.30 | 29.443 | 31.588 | 3.419 | 0.838 | 0.905 | 8.746 | 28.579 | 154 | 3520957 |
| 12.54 | 30.061 | 34.098 | 3.167 | 0.818 | 0.889 | 10.368 | 30.323 | 116 | 3350116 |
| 10.73 | 28.279 | 27.751 | 3.892 | 0.870 | 0.927 | 9.451 | 25.729 | 176 | 2630748 |
| 8.23 | 32.109 | 46.630 | 2.316 | 0.726 | 0.806 | 6.071 | 37.597 | 129 | 8844517 |
| 11.65 | 31.862 | 44.609 | 2.421 | 0.740 | 0.820 | 8.713 | 36.584 | 95 | 5832006 |
| 11.00 | 31.529 | 42.177 | 2.561 | 0.757 | 0.837 | 8.422 | 35.284 | 106 | 5607258 |
| 9.92 | 31.313 | 40.738 | 2.651 | 0.767 | 0.846 | 7.711 | 34.473 | 121 | 5842552 |
| 7.19 | 29.589 | 32.146 | 3.360 | 0.834 | 0.901 | 6.107 | 28.975 | 215 | 5185685 |

**Figure C-1 Cumulative Percentage Plot of the PCC Elastic Modulus**

APPENDIX D

Westergaard's Calculation for the "Equivalent" Plate of an Unbonded AC/PCC Pavement in which, "1" indicates the AC properties and "2" indicates the PCC properties.

$$P := 9000$$

$$\mu := .35$$

$$k := 151$$

$$a := 6.77$$

$$f_c := 4500$$

$$E1 := 1354679$$

$$E2 := 3100000$$

$$E := E1 \rightarrow 1354679$$

$$h1 := 5$$

$$h2 := 7.0$$

Two Layers - Unbonded Condition

$$h_e := \left[\left(\frac{E1}{E} \right) \cdot h1^3 + \left(\frac{E2}{E} \right) \cdot h2^3 \right]^{\frac{1}{3}} \quad h_e = 9.69$$

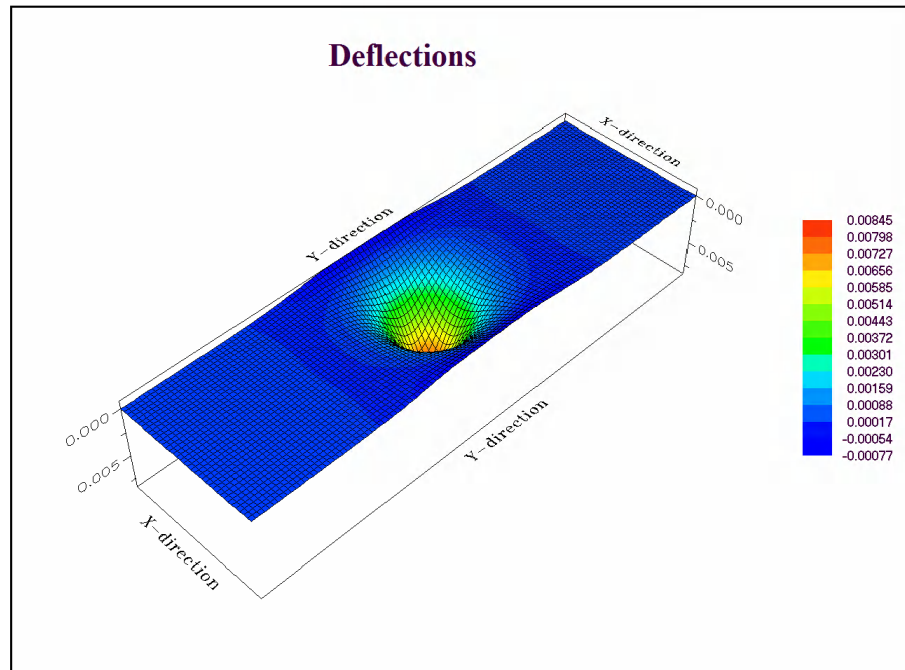
$$L := \left[\frac{(E \cdot h_e^3)}{12(1 - \mu^2) \cdot k} \right]^{.25} \quad L = 29.673$$

Interior Loading - Unbonded

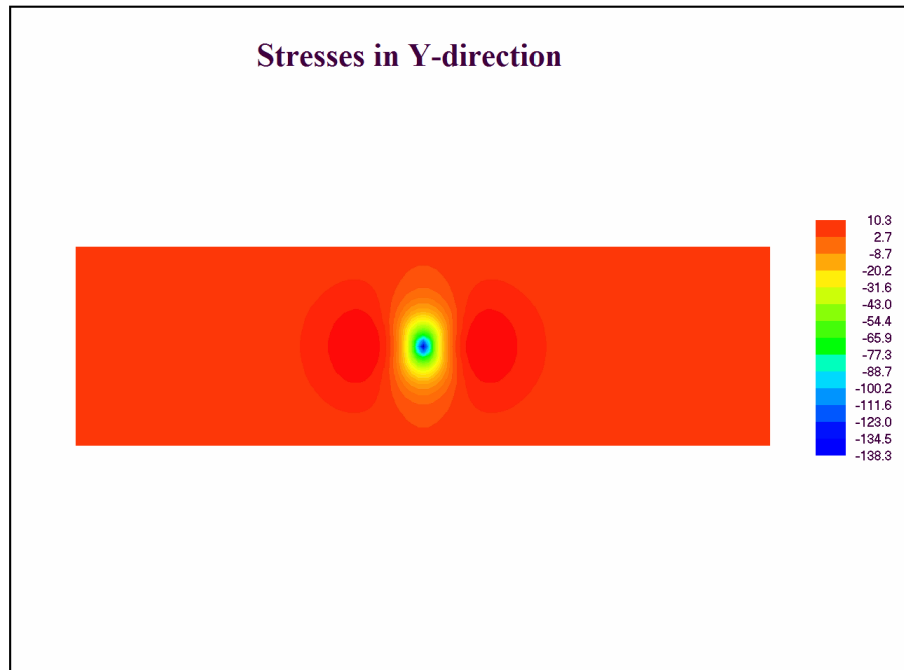
$$b := \sqrt{(1.6 \cdot a^2 + h_e^2)} - 0.675 \cdot h_e \quad b = 6.391$$

$$\sigma_e := \frac{[3 \cdot (1 + \mu) \cdot P]}{[3.14159 \cdot (2) \cdot h_e^2]} \cdot \left[\ln \left[\frac{(L)}{b} \right] + 0.6159 \right] \quad \sigma_e = 132.905$$

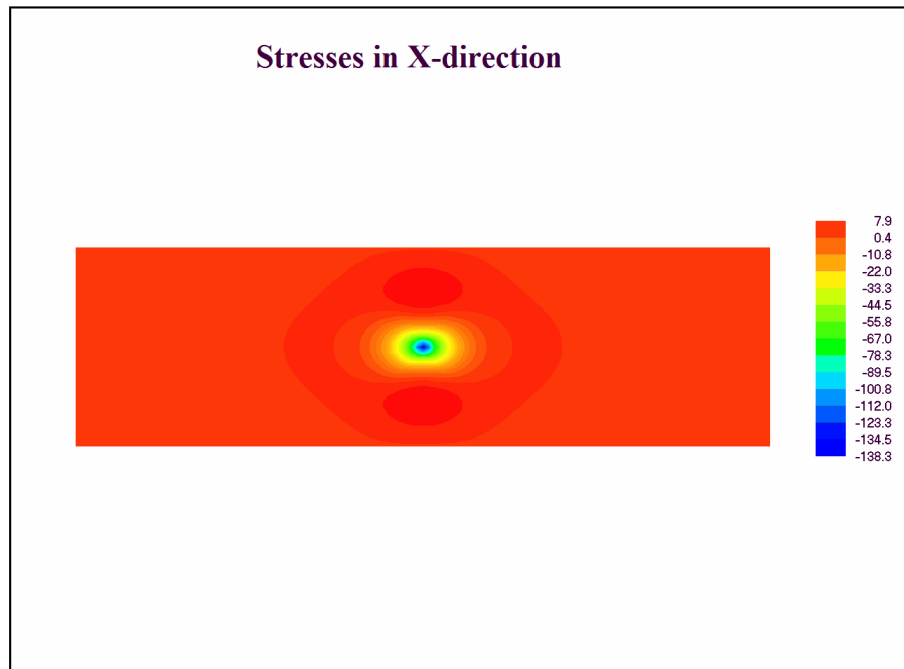
$$\Delta e := \left(\frac{P}{8 \cdot k \cdot L^2} \right) \cdot \left[1 + \left(\frac{1}{2 \cdot 3.14159} \right) \cdot \left(\ln \left(\frac{a}{2 \cdot L} \right) - 0.673 \right) \cdot \left(\frac{a}{L} \right)^2 \right] \quad \Delta e = 0.00826$$



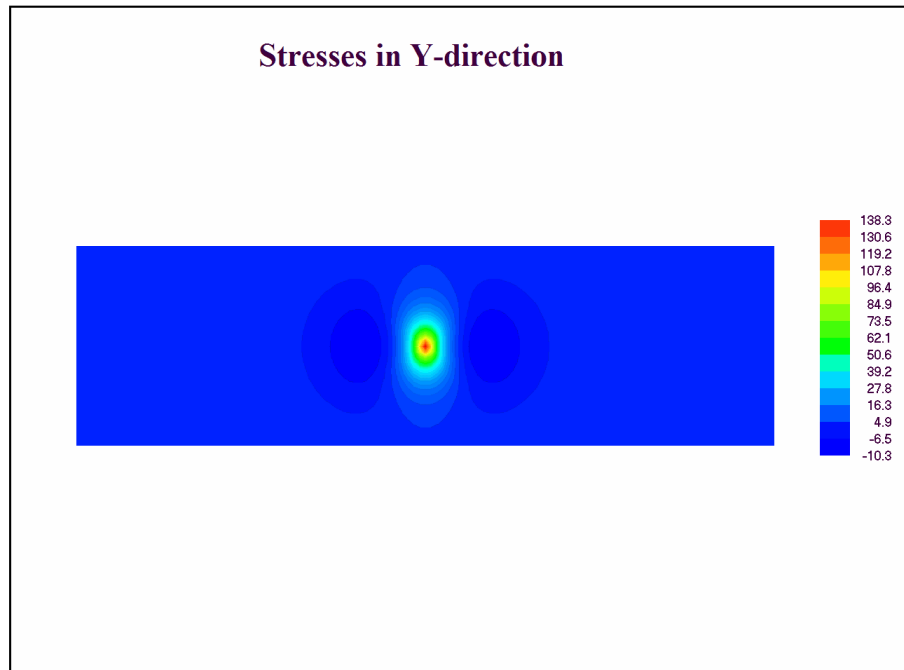
**Figure X-X Deflected Shape, “equivalent” Slab Thickness, $h_e=9.6$ inches, $CL = 62.5$ psi,
ISLAB2000 Graphical Output**



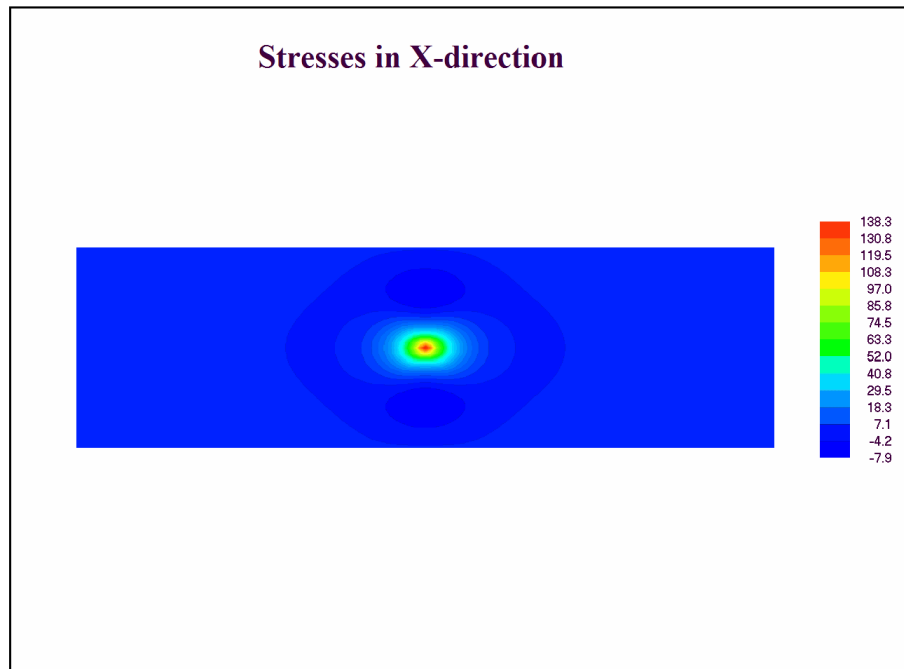
**Figure X-X Longitudinal Stress, Top of “equivalent” Slab, $h_e=9.6$ inches, $CL = 62.5$ psi,
ISLAB2000 Graphical Output**



**Figure X-X Transverse Stress, Top of “equivalent” Slab, $h_e=9.6$ inches, $CL = 62.5$ psi,
ISLAB2000 Graphical Output**



**Figure X-X Longitudinal Stress, Bottom of “equivalent” Slab Thickness, $h_e=9.6$ inches,
CL = 62.5 psi, ISLAB2000 Graphical Output**



**Figure X-X Transverse Stress, Bottom of “equivalent” Slab Thickness, CL = 62.5 psi,
ISLAB2000 Graphical Output**

APPENDIX E

Westergaard's Calculation for the "Equivalent" Plate of an Unbonded AC/PCC Pavement in which, "1" indicates the AC properties and "2" indicates the PCC properties.

$$P := 9000$$

$$\mu := .35$$

$$k := 151$$

$$a := 6.77$$

$$fc := 4500$$

$$E1 := 1354680$$

$$E2 := 3100000$$

$$E := E1 \rightarrow 1354680$$

$$h1 := 5$$

$$h2 := 7.0$$

Two Layered - Unbonded Condition

$$he := \left[\left(\frac{E1}{E} \right) \cdot h1^3 + \left(\frac{E2}{E} \right) \cdot h2^3 \right]^{\frac{1}{3}}$$

$$he = 9.69$$

$$L := \left[\frac{(E \cdot he^3)}{12(1 - \mu^2) \cdot k} \right]^{.25}$$

$$L = 29.673$$

Interior Loading - Unbonded

$$b := \sqrt{(1.6 \cdot a^2 + he^2)} - 0.675 \cdot he$$

$$b = 6.391$$

$$\sigma_e := \frac{[3 \cdot (1 + \mu) \cdot P]}{[3.14159 \cdot (2) \cdot he^2]} \cdot \left[\ln \left[\frac{(L)}{b} \right] + 0.6159 \right]$$

$$\sigma_e = 132.905$$

$$\Delta e := \left(\frac{P}{8 \cdot k \cdot L^2} \right) \cdot \left[1 + \left(\frac{1}{2 \cdot 3.14159} \right) \cdot \left(\ln \left(\frac{a}{2 \cdot L} \right) - 0.673 \right) \cdot \left(\frac{a}{L} \right)^2 \right]$$

$$\Delta e = 0.00826$$

Stresses in the bottom of each layer (Ioannides)

$$\sigma_1 := \left(\frac{h_1}{h_e} \right) \cdot \sigma_e$$

$$\sigma_1 = 68.577$$

$$\sigma_2 := \left(\frac{h_2}{h_1} \right) \cdot \left(\frac{E_2}{E_1} \right) \sigma_1$$

$$\sigma_2 = 219.701$$

Westergaard's Calculation for the "Equivalent" Plate of a Bonded AC/PCC Pavement in which, "2" indicates the AC properties and "1" indicates the PCC properties.

Bonded Condition

$$E2 := 1354680$$

$$E1 := 3100000$$

$$E := E1 \rightarrow 3100000$$

$$h2 := 5$$

$$h1 := 7.0$$

$$x := \frac{E1 \cdot h1 \cdot \left(\frac{h1}{2}\right) + E2 \cdot h2 \cdot \left(h1 + \frac{h2}{2}\right)}{E1 \cdot h1 + E2 \cdot h2}$$

$$x = 4.927$$

$$he := \left[\frac{12}{E} \left[E1 \cdot h1 \cdot \left(x - \frac{h1}{2}\right)^2 + \left(\frac{E1 \cdot h1^3}{12}\right) + E2 \cdot h2 \cdot \left(h1 - x + \frac{h2}{2}\right)^2 + \frac{E2 \cdot h2^3}{12} \right] \right]^{\frac{1}{3}}$$

$$he = 10.376$$

$$L := \left[\frac{(E \cdot he^3)}{[12(1 - \mu^2) \cdot k]} \right]^{.25}$$

$$L = 38.415$$

Interior Loading Bonded

$$b := \sqrt{(1.6 \cdot a^2 + he^2)} - 0.675 \cdot he$$

$$b = 6.45$$

$$\sigma_e := \frac{[3 \cdot (1 + \mu) \cdot P]}{[3.14159 \cdot (2) \cdot he^2]} \cdot \left[\ln \left[\frac{(L)}{b} \right] + 0.6159 \right]$$

$$\sigma_e = 129.347$$

$$\Delta e := \left(\frac{P}{8 \cdot k \cdot L^2} \right) \cdot \left[1 + \left(\frac{1}{2 \cdot 3.14159} \right) \cdot \left(\ln \left(\frac{a}{2 \cdot L} \right) - 0.673 \right) \cdot \left(\frac{a}{L} \right)^2 \right]$$

$$\Delta e = 0.00497$$

Stresses in the bottom of each layer (Ioannides)

$$y := h1 - x$$

$$y = 2.073$$

$$\sigma_{1\text{top}} := \frac{2 \cdot (h1 - x)}{h_e} \cdot \sigma_e$$

$$\sigma_{1\text{top}} = 51.678$$

$$\sigma_{1\text{bottom}} := \left(\frac{x}{h1 - x} \right) \cdot \sigma_{1\text{top}}$$

$$\sigma_{1\text{bottom}} = 122.852$$

$$\sigma_{2\text{top}} := \sigma_{1\text{top}} \cdot \left(\frac{E2}{E} \right) \cdot \frac{(h2 + h1 - x)}{x}$$

$$\sigma_{2\text{top}} = 32.416$$

$$\sigma_{2\text{bottom}} := \sigma_{1\text{top}} \cdot \frac{E2}{E}$$

$$\sigma_{2\text{bottom}} = 22.583$$

APPENDIX F

Closed form Calculations for the “Equivalent” Plate and Stress distribution of an Unbonded and Bonded PCC Overlay/AC/PCC Pavement in which, “1” indicates the PCC Overlay properties, “2” indicates the AC properties and “3” indicates existing PCC properties.

P := 9000
 μ := .15
k := 150
a := 6
fc := 4500
E1 := 3823680
E2 := 1354679
E3 := 3100000
E := E1 \rightarrow 3823680
h1 := 3.5
h2 := 5
h3 := 7

Interior Loading - Unbonded

$$h_e := \left[\left(\frac{E1}{E} \right) \cdot h1^3 + \left(\frac{E2}{E} \right) \cdot h2^3 + \left(\frac{E3}{E} \right) \cdot h3^3 \right]^{\frac{1}{3}}$$

$$h_e = 7.148$$

$$L := \left[\frac{(E \cdot h_e^3)}{[12(1 - \mu) \cdot k]} \right]^{.25}$$

$$L = 30.91$$

$$b := \sqrt{(1.6 \cdot a^2 + h_e^2)} - 0.675 \cdot h_e$$

$$b = 5.601$$

$$\sigma_e := \frac{[3 \cdot (1 + \mu) \cdot P]}{[3.14159 \cdot (2) \cdot h_e^2]} \cdot \left[\ln \left[\frac{(L)}{b} \right] + 0.6159 \right]$$

$$\sigma_e = 224.772$$

$$\Delta e := \left(\frac{P}{8 \cdot k \cdot L^2} \right) \cdot \left[1 + \left(\frac{1}{2 \cdot 3.14159} \right) \cdot \left(\ln \left(\frac{a}{2 \cdot L} \right) - 0.673 \right) \cdot \left(\frac{a}{L} \right)^2 \right]$$

$$\Delta e = 0.00771$$

Stresses in the bottom of each layer (Ioannides)

$$\sigma_1 := \frac{h_1}{h_e} \cdot \sigma_e$$

$$\sigma_1 = 110.057$$

$$\sigma_2 := \frac{h_2}{h_1} \cdot \left(\frac{E_2}{E_1} \right) \cdot \sigma_1$$

$$\sigma_2 = 55.702$$

$$\sigma_3 := \frac{h_3}{h_1} \cdot \left(\frac{E_3}{E_1} \right) \cdot \sigma_1$$

$$\sigma_3 = 178.454$$

Interior Loading - Bonded

$$E_1 := 3823680$$

$$E_2 := 1354679$$

$$E_3 := 3100000$$

$$E := E_2 \rightarrow 1354679$$

$$h_1 := 3.5$$

$$h_2 := 5$$

$$h_3 := 7$$

$$x := \frac{E_1 \cdot h_1 \cdot \left(\frac{h_1}{2} \right) + E_2 \cdot h_2 \cdot \left(h_1 + \frac{h_2}{2} \right) + E_3 \cdot h_3 \cdot \left[h_1 + h_2 + \left(\frac{h_3}{2} \right) \right]}{E_1 \cdot h_1 + E_2 \cdot h_2 + E_3 \cdot h_3}$$

$$x = 7.752$$

$$h_e := \left[\frac{12}{E} \cdot \left[\left[x - \left(\frac{h_1}{2} \right) \right]^2 \cdot E_1 \cdot h_1 + \frac{(E_1 \cdot h_1^3)}{12} + \frac{(E_2 \cdot h_2^3)}{12} + E_2 \cdot h_2 \cdot \left[h_1 - x + \left(\frac{h_2}{2} \right) \right]^2 + \frac{(E_3 \cdot h_3^3)}{12} + E_3 \cdot h_3 \cdot \left[h_1 + h_2 - x + \left(\frac{h_3}{2} \right) \right]^2 \right] \right]^{\frac{1}{3}}$$

$$h_e = 20.766$$

$$L := \left[\frac{(E \cdot h e^3)}{12(1 - \mu^2) \cdot k} \right]^{.25}$$

$$L = 51.241$$

$$b := \sqrt{(1.6 \cdot a^2 + h e^2)} - 0.675 \cdot h e$$

$$b = 8.092$$

$$\sigma e := \frac{[3 \cdot (1 + \mu) \cdot P]}{[3.14159 \cdot (2) \cdot h e^2]} \cdot \left(\ln\left(\frac{L}{b}\right) + 0.6159 \right)$$

$$\sigma e = 28.21$$

$$\Delta e := \left(\frac{P}{8 \cdot k \cdot L^2} \right) \cdot \left[1 + \left(\frac{1}{2 \cdot 3.14159} \right) \cdot \left(\ln\left(\frac{a}{2 \cdot L}\right) - 0.673 \right) \cdot \left(\frac{a}{L} \right)^2 \right]$$

$$\Delta e = 0.00283$$

Stresses in the each layer (Ioannides)

$$y := h1 + h2 - x$$

$$y = 0.748$$

$$\sigma_{2bottom} := \left[\frac{2 \cdot (h1 + h2 - x)}{h e} \right] \cdot \sigma e$$

$$\sigma_{2bottom} = 2.033$$

$$\sigma_{2top} := \left(\frac{x - h1}{h1 + h2 - x} \right) \cdot \sigma_{2bottom}$$

$$\sigma_{2top} = 11.552$$

$$\sigma_{1top} := \frac{x}{h2 - y} \cdot \left(\frac{E1}{E} \right) \cdot \sigma_{2top}$$

$$\sigma_{1top} = 59.447$$

$$\sigma_{1bottom} := \left(\frac{E1}{E} \right) \cdot \sigma_{2top}$$

$$\sigma_{1\text{bottom}} = 32.606$$

$$\sigma_{3\text{top}} := \left(\frac{E_3}{E}\right) \cdot \sigma_{2\text{bottom}}$$

$$\sigma_{3\text{top}} = 4.652$$

$$\sigma_{3\text{bottom}} := \left(\frac{h_3 + y}{y}\right) \left(\frac{E_3}{E}\right) \cdot \sigma_{2\text{bottom}}$$

$$\sigma_{3\text{bottom}} = 48.173$$

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